

Height System Unification with SAR/SARin

Cryosat-2 SAR and SARin contribution to Height System Unification in Greece

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IAG-IASPEI 2017

Session G2.6

Kobe, Japan
August 1, 2017



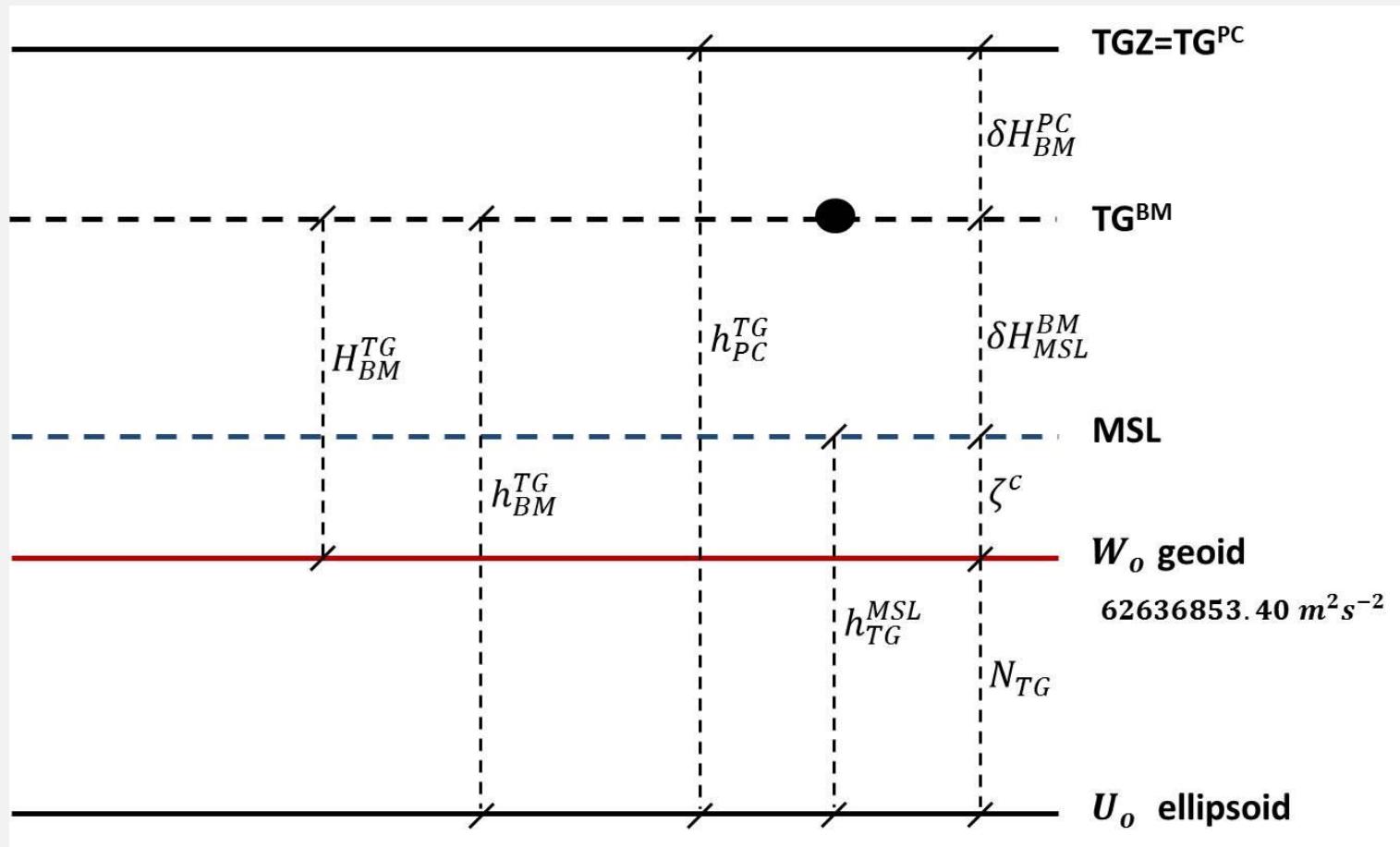
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Rationale and outline

- For HSU ellipsoidal heights at BMs and/or TGs are needed
- Only a few number of TGs have collocated GNSS observations (SONEL)
-while many areas do not have GNSS infrastructure at all
- Nevertheless, HSU is needed as a tool for scientific and mainly engineering applications
- Satellite altimetry provides the opportunity to estimate ellipsoidal heights (almost) all over the world, irrespective of site location

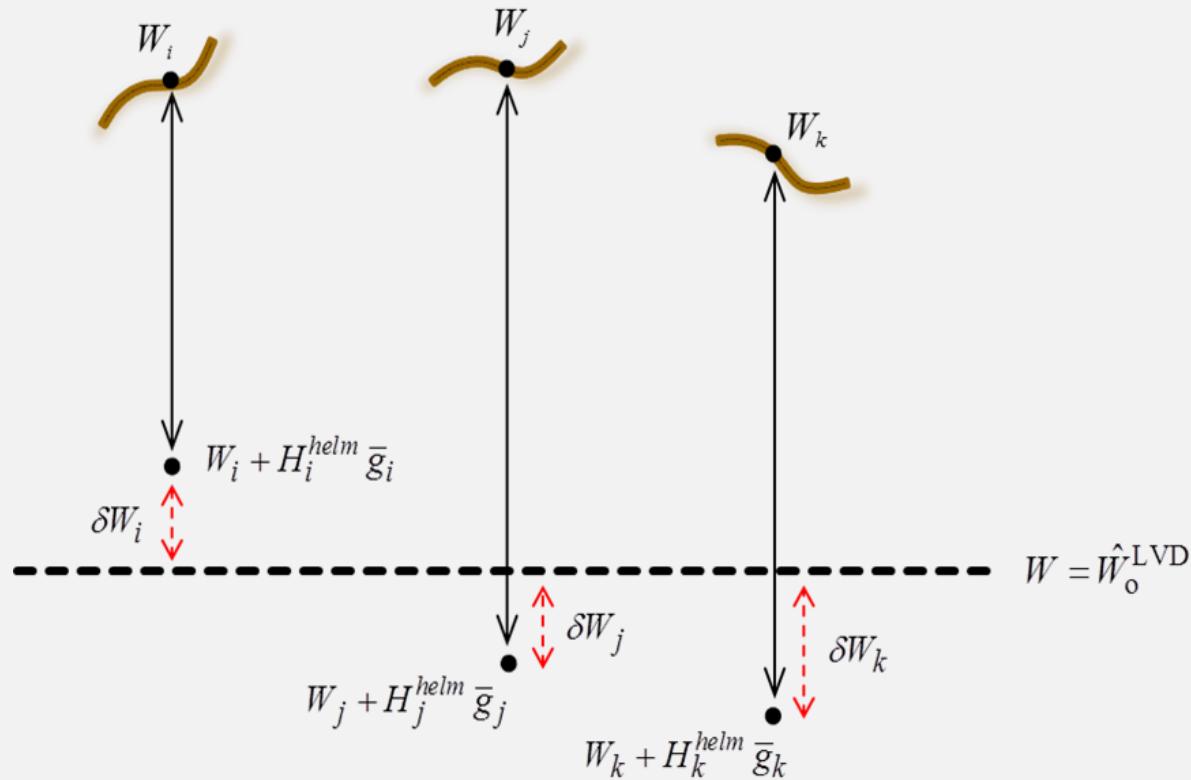
Necessity of the project and goals

To define the VRS and realize the VRF, link with ellipsoidal heights at the TG locations is needed



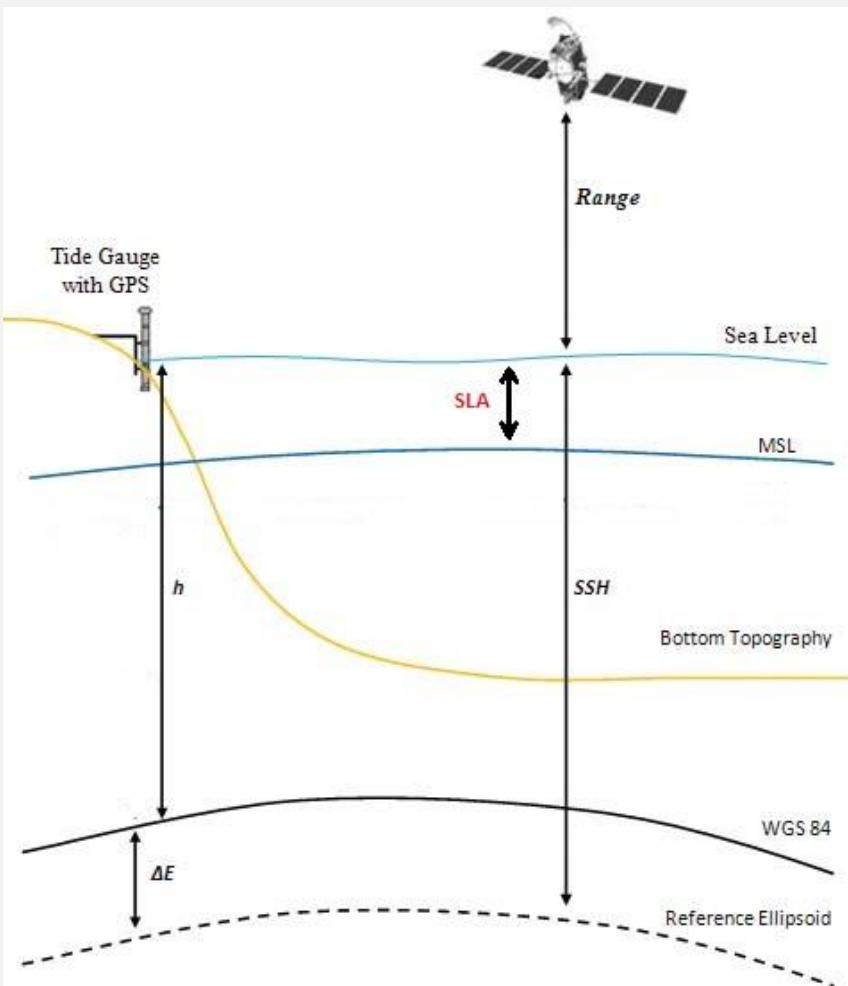
Necessity of the project and goals

Then HSU can be carried out employing all leveling, geoid, gravity, and TG data



Zero-height geopotential value determination from a network of stations
(after Grigoriadis et al. 2014)

Data availability



Singh et al. (2013)

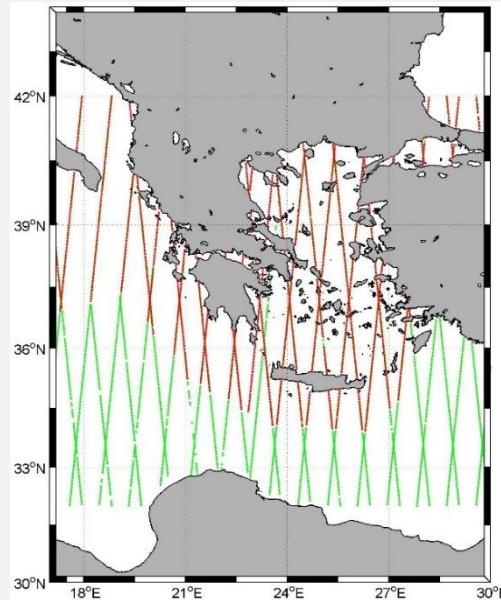
SLA values (August 2010 – December 2016)

LRM (2010-2015) - RADS

SAR (2010-2015) - SARVATORE

SARin (2016) - SARVATORE

Cycle 36

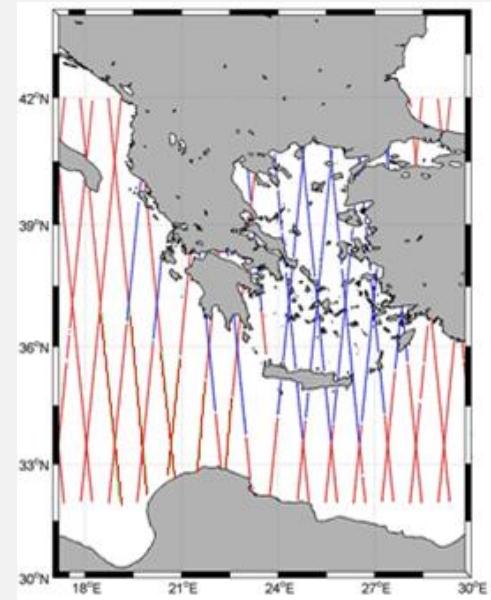


LRM

SAR

SARin

Cycle 75 until now



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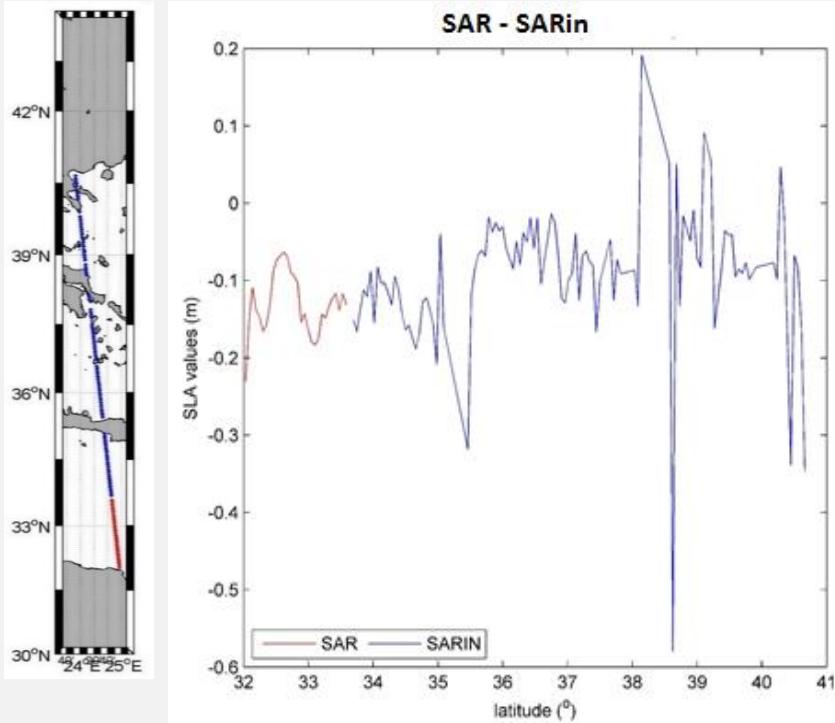
Data availability

- RADS : all corrections - except IB
- SARVATORE : all corrections - except IB/SSB
- SARVATORE Processing Options: Zero-padding, extended analysis window (256 range bins), re-tracking on coastal zone
- IB corrected - SLA values [-0.5,0.5] m → rejected

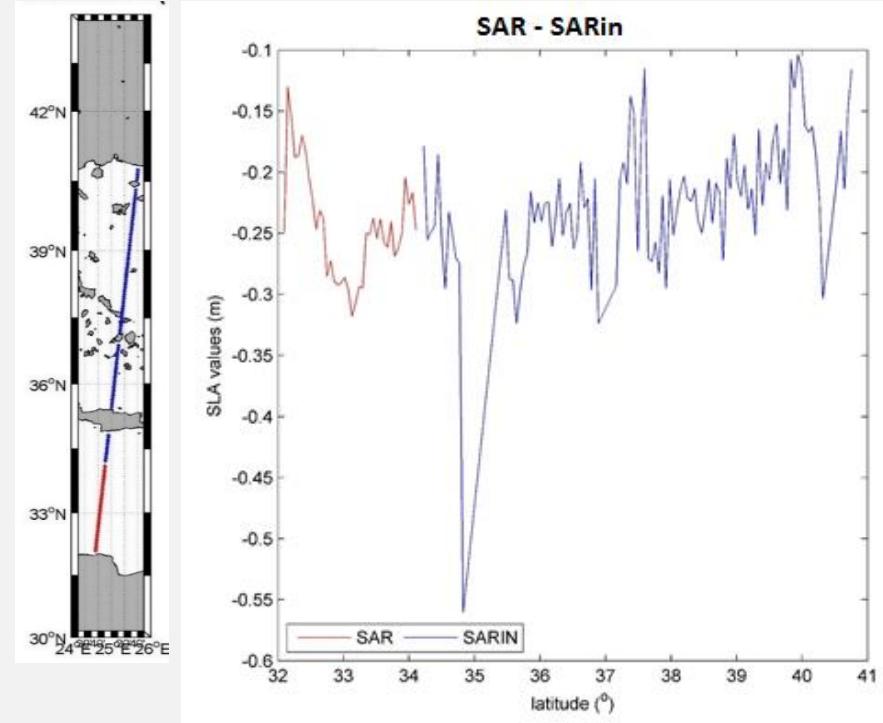
[cm]	LRM [171143]	SAR [111792]	SARin [11570]
min	-50.00	-49.99	-49.79
max	49.60	49.66	49.81
mean	-2.64	-7.33	-11.04
std	12.71	13.33	12.44
rms	12.99	15.21	16.63

Bias investigation between

➤ SAR and SARin modes



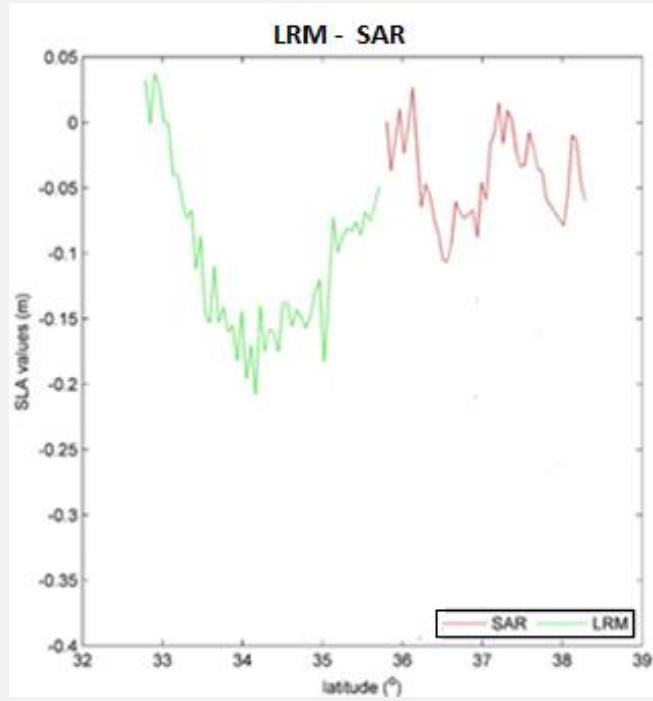
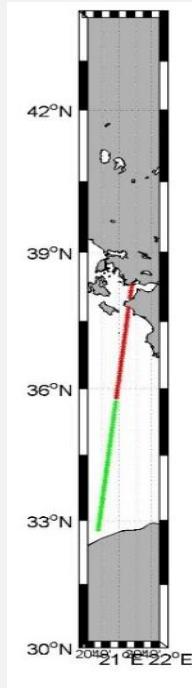
Cycle 74 – pass 738



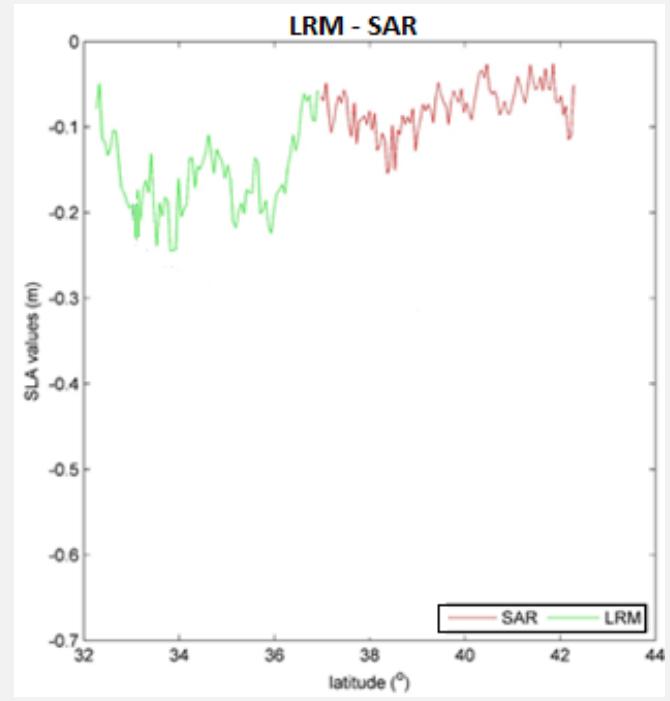
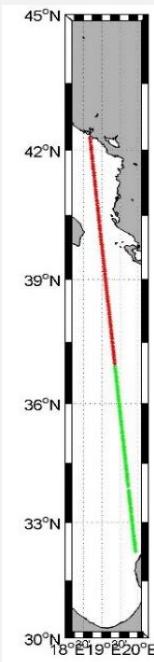
Cycle 74 – pass 607

Bias investigation between

➤ SAR and LRM modes



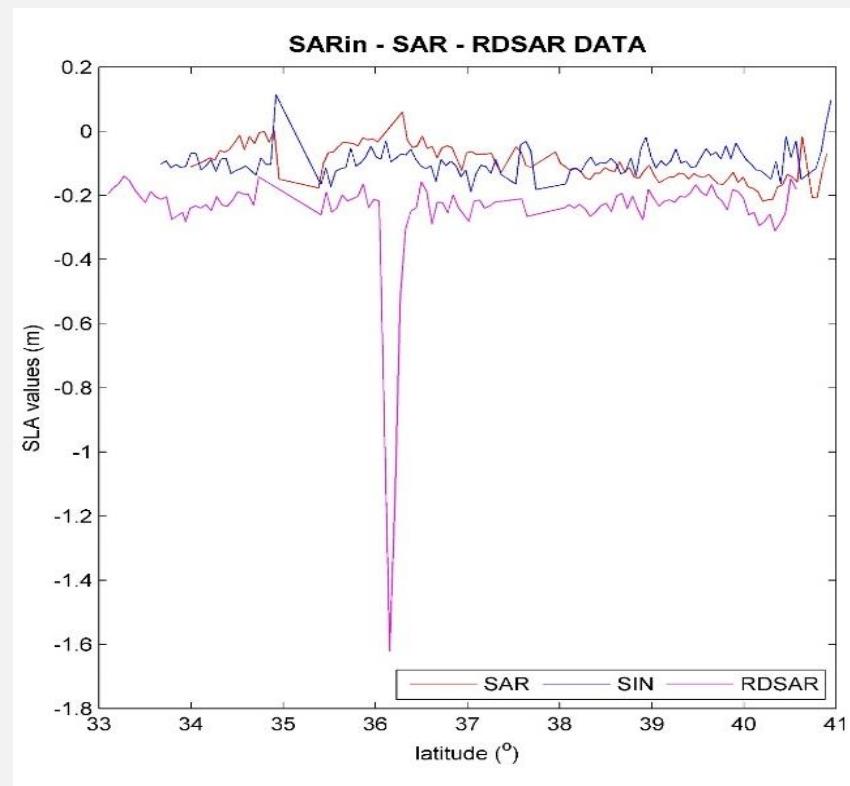
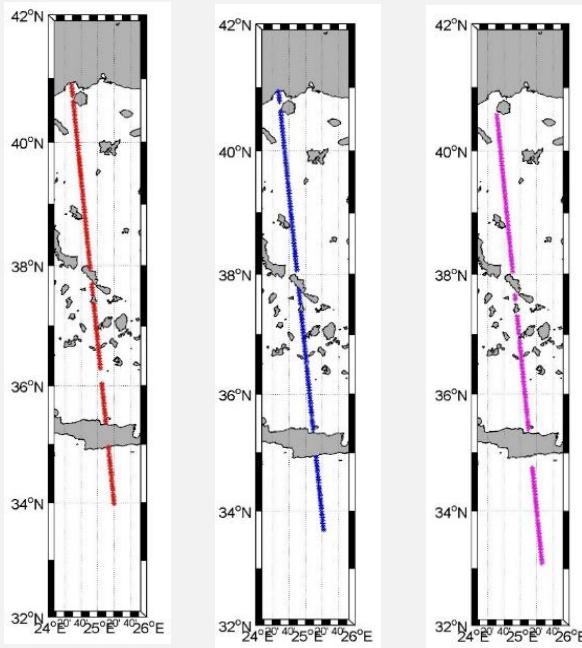
Cycle 74 – pass 188



Cycle 74 – pass 173

Evaluation of SAR – SARin – RDSAR data in Greece

January : cycle 36 (SAR, RDSAR) - cycle 75 (SARin)



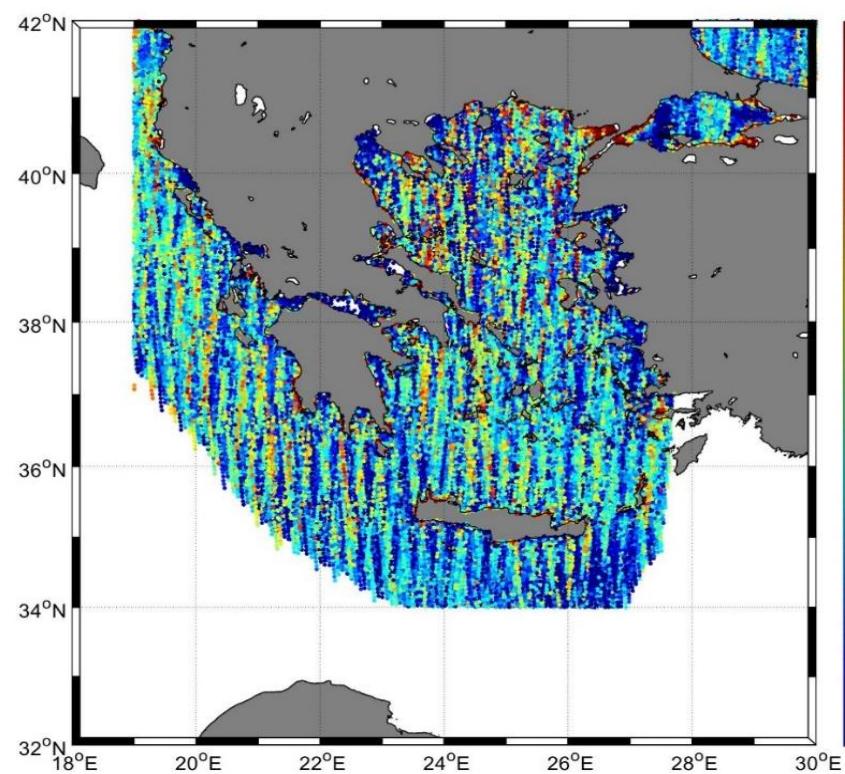
Evaluation of SAR – SARin – RDSAR data in Greece

[cm]	#607 - January			#607 - February		
	2013 – cycle 36		2016 – cycle 75	2013 – cycle 37		2016 – cycle 76
	RDSAR	SAR	SARin	RDSAR	SAR	SARin
min	-162.20	-21.87	-18.98	-31.31	-55.34	-30.24
max	-14.00	5.90	11.43	0.70	2.17	1.02
std	± 17.83	± 5.58	± 4.44	± 5.33	± 6.14	± 6.28
mean	-25.28	-10.03	-9.62	-18.98	-13.64	-13.09
rms	± 30.94	± 11.47	± 10.59	± 19.54	± 14.96	± 14.52

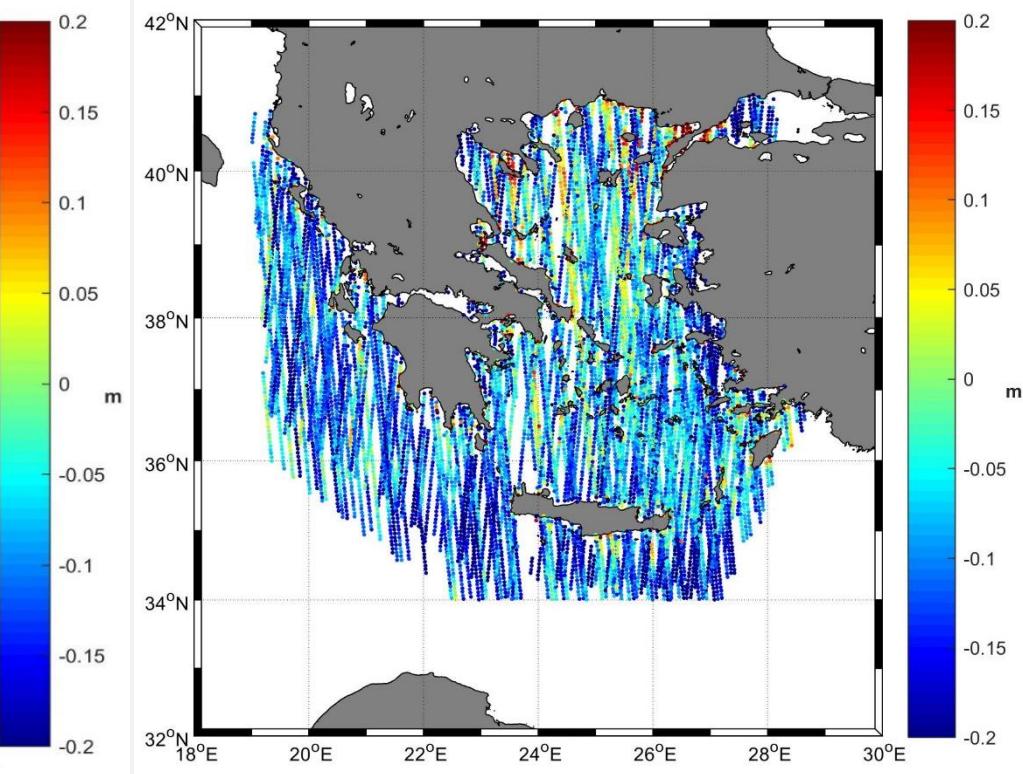
[cm]	#738 - March			#607 - April		
	2013 – cycle 38		2016 – cycle 77	2013 – cycle 39		2016 – cycle 78
	RDSAR	SAR	SARin	RDSAR	SAR	SARin
min	-11.50	-74.26	-130.29	-100.60	-24.21	-26.26
max	29.10	13.72	25.54	9.80	9.34	6.92
std	± 6.92	± 8.78	± 13.07	± 12.80	± 4.75	± 5.77
mean	5.94	-6.00	-16.99	-7.36	-5.51	-2.47
rms	± 9.12	± 10.64	± 21.44	± 14.77	± 7.28	± 6.28

[cm]	#738 - May		
	2013 – cycle 40		2016 – cycle 79
	RDSAR	SAR	SARin
min	-123.10	-99.37	-44.36
max	18.30	9.94	13.23
std	± 13.84	± 10.39	± 7.48
mean	-5.36	-10.31	-12.79
rms	± 14.84	± 14.64	± 14.82

Cryosat-2 Data in the Aegean Sea 2010 - 2016



$\sigma_{\text{SAR}} = 11.01 \text{ cm}$
~ 111000 pts.



$\sigma_{\text{SARin}} = 9.24 \text{ cm}$
~ 11000 pts.

Ellipsoidal height prediction at BMs

- 1D low pass filtering
- 2D low pass filtering
- Non-corrected SSB
- SSB corrected -> 4% SWH
- Linear – Nearest – Cubic interpolation

Prediction methods

- ✓ Cubic interpolation
- ✓ Least Squares Collocation

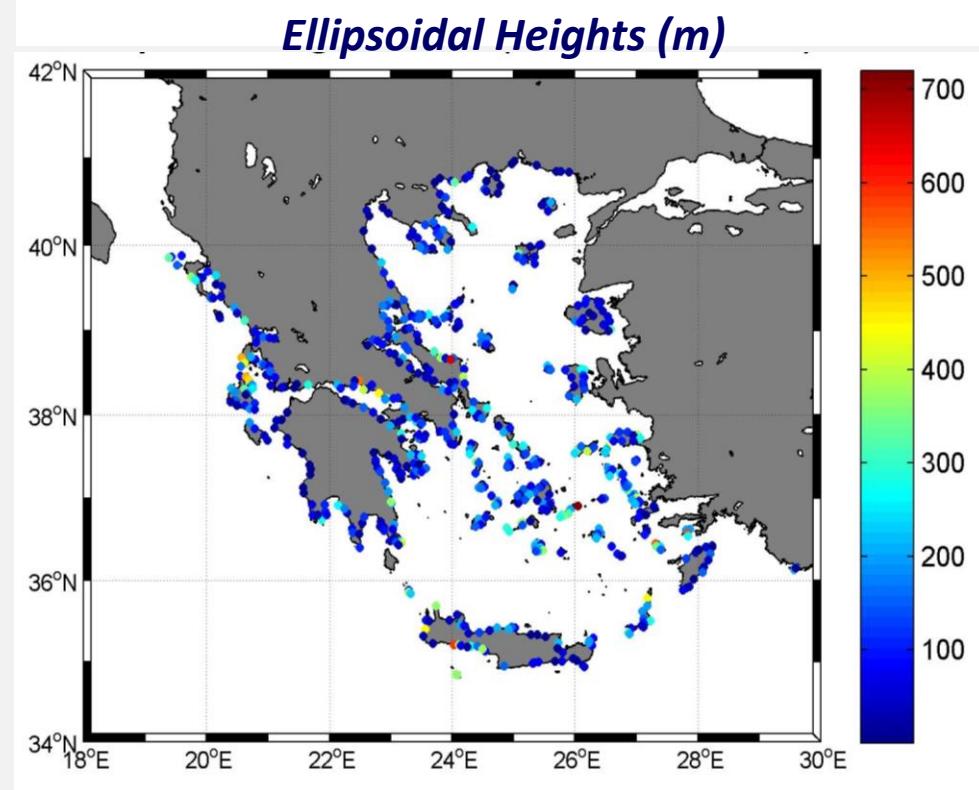
Ellipsoidal height prediction at BMs

602 BMs – 1 km from coastline

- Orthometric Heights : Helmert-type

$\sigma_H = 0.1\text{-}1 \text{ cm (1}\sigma\text{) (formal)}$

$\sigma_H = 3\text{-}8 \text{ cm (1}\sigma\text{) (realistic – a-posteriori)}$



- Ellipsoidal Heights : GPS measurements

(Hepos project, 2008)

$\sigma_{\text{hor}} = 1\text{-}4 \text{ cm (1}\sigma\text{)}$

$\sigma_{\text{vert}} = 2\text{-}5 \text{ cm (1}\sigma\text{)}$

$$\hat{h} = \text{MSS} + \text{SLA} + H$$

Cubic interpolation

- A) 2D FILTERING – GRID 3' – INTERPOLATION SLAs AT BMs – ADD MSS AT BMs
- B) 2D FILTERING – GRID 3' – ADD MSS AT GRID – INTERPOLATION MSS+SLA AT BMs
- C) GRID 3' – INTERPOLATION SLAs AT BMs – ADD MSS AT BMs
- D) GRID 3' – ADD MSS AT GRID – INTERPOLATION MSS+SLA AT BMs
- E) GRID 3' – 2D FILTERING – INTERPOLATION SLAs AT BMs – ADD MSS AT BMs
- F) GRID 3' – 2D FILTERING – ADD MSS AT GRID – INTERPOLATION MSS+SLA AT BMs

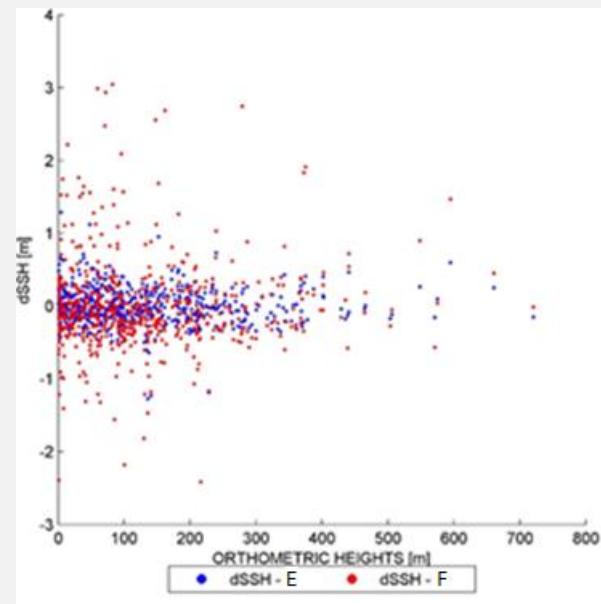
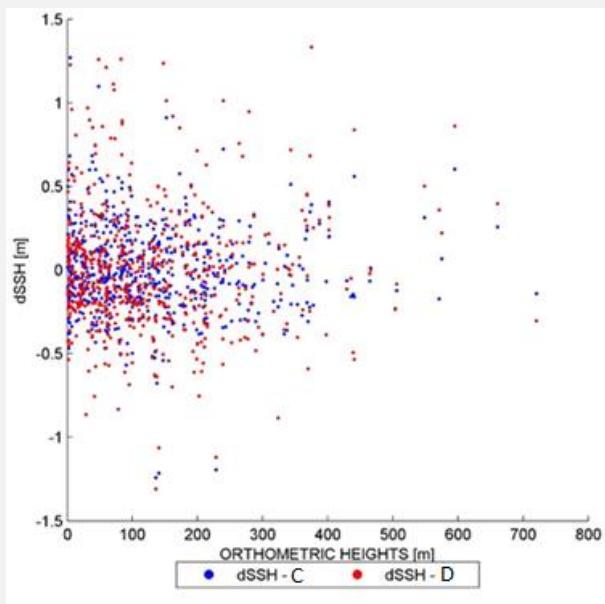
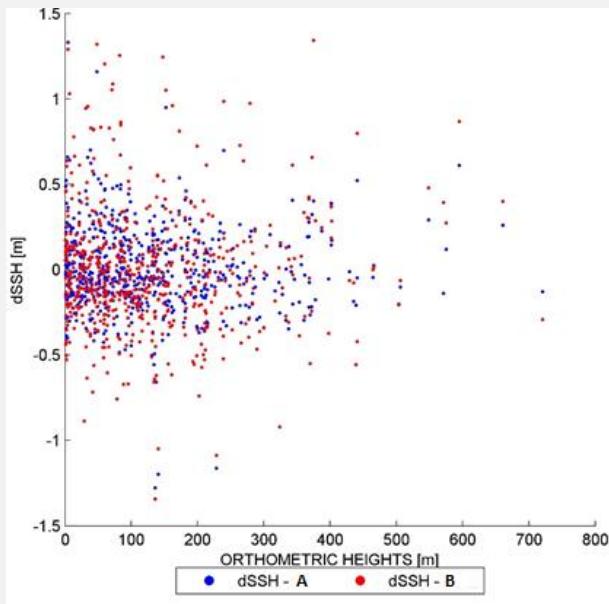
Ellipsoidal height prediction at BMs

Cubic interpolation

[cm]	A		B		C	
std	± 23.76		± 24.00		± 25.72	
mean	-74.14		-71.91		-71.85	
	$\pm 10 \text{ cm}$ [40.86%]	$\pm 20 \text{ cm}$ [69.77%]	$\pm 10 \text{ cm}$ [39.87%]	$\pm 20 \text{ cm}$ [69.10%]	$\pm 10 \text{ cm}$ [33.22%]	$\pm 20 \text{ cm}$ [62.79%]
std	± 5.75	± 10.22	± 5.74	± 10.32	± 5.81	± 10.97
mean	-0.87	-2.65	-0.76	-2.52	-0.95	-2.07
rms	± 5.82	± 10.56	± 5.79	± 10.62	± 5.89	± 11.16
<hr/>						
[cm]	D		E		F	
std	± 35.84		± 24.93		± 61.71	
mean	-67.76		-74.26		-60.34	
	$\pm 10 \text{ cm}$ [24.42%]	$\pm 20 \text{ cm}$ [51.16%]	$\pm 10 \text{ cm}$ [41.80%]	$\pm 20 \text{ cm}$ [70.02%]	$\pm 10 \text{ cm}$ [21.59%]	$\pm 20 \text{ cm}$ [37.54%]
std	± 5.45	± 11.49	± 5.12	± 10.69	± 5.70	± 11.04
mean	-0.63	-0.94	-1.01	-1.81	-0.72	-1.71
rms	± 5.49	± 11.53	± 5.22	± 10.84	± 5.75	± 11.17

Ellipsoidal height prediction at BMs

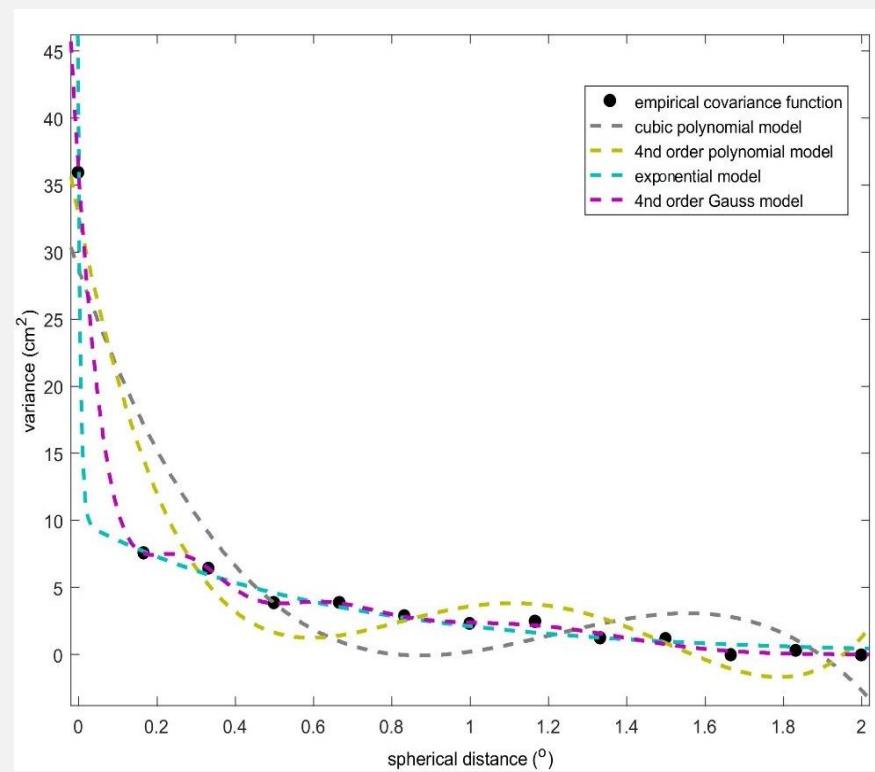
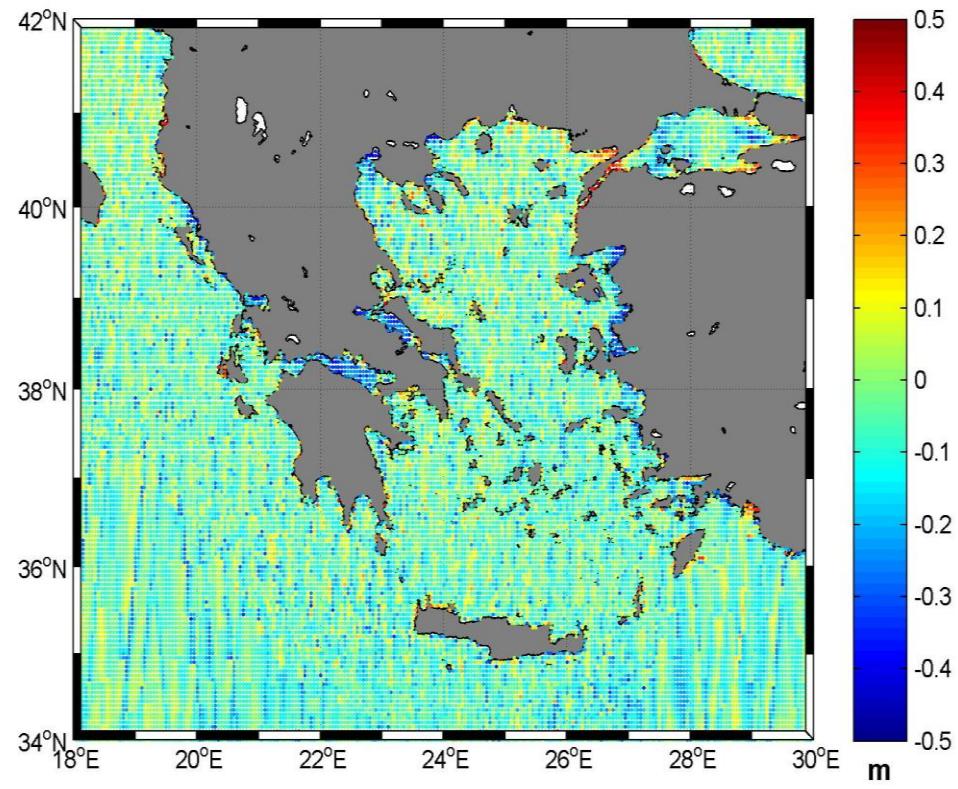
Cubic interpolation – Differences between predicted and initial SLA values



no correlation between prediction accuracy and topography

Ellipsoidal height prediction at BMs

Least Squares Collocation – Gridded data (CASE E)



Ellipsoidal height prediction at BMs

Least Squares Collocation – Gridded data (CASE E)

Remove Local Vertical Offset : -74.26 cm

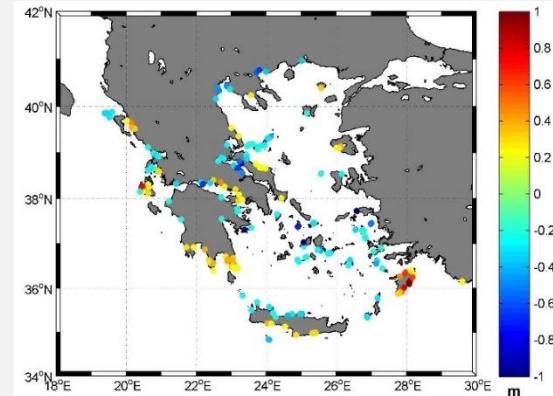
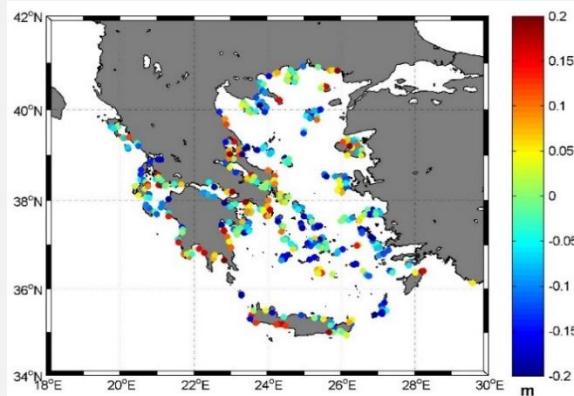
[cm]	Exponential model		3rd order polynomial model		4th order polynomial model		4th order Gauss model	
std	± 23.45		± 26.01		± 25.49		± 23.46	
mean	-77.63		-75.83		-75.67		-77.64	
	$\pm 10 \text{ cm}$ [42.03%]	$\pm 20 \text{ cm}$ [69.77%]	$\pm 10 \text{ cm}$ [37.20%]	$\pm 20 \text{ cm}$ [62.46%]	$\pm 10 \text{ cm}$ [36.54%]	$\pm 20 \text{ cm}$ [62.46%]	$\pm 10 \text{ cm}$ [42.03%]	$\pm 20 \text{ cm}$ [69.77%]
std	± 5.47	± 10.18	± 10.41	± 10.32	± 5.89	± 10.19	± 5.48	± 10.18
mean	-0.59	-2.56	-1.14	-2.30	-0.39	-2.39	-0.59	-2.57
rms	± 5.50	± 10.50	± 10.48	± 10.57	± 5.90	± 10.47	± 5.51	± 10.50

Remove Local Vertical Offset : - 64.91 cm

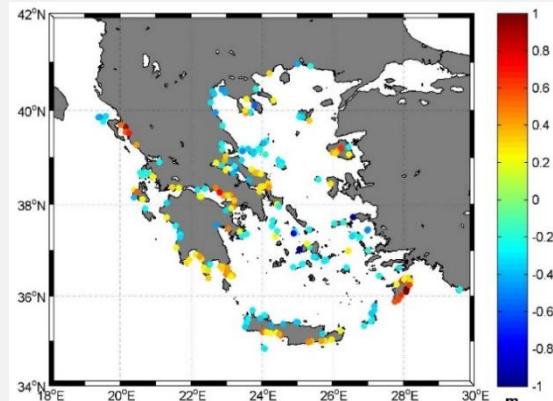
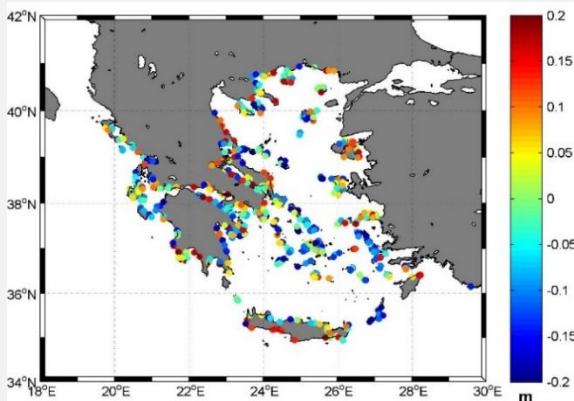
[cm]	Exponential model		3rd order polynomial model		4th order polynomial model		4th order Gauss model	
	$\pm 10 \text{ cm}$ [29.73%]	$\pm 20 \text{ cm}$ [57.97%]	$\pm 10 \text{ cm}$ [25.91%]	$\pm 20 \text{ cm}$ [53.32%]	$\pm 10 \text{ cm}$ [25.41%]	$\pm 20 \text{ cm}$ [53.65%]	$\pm 10 \text{ cm}$ [29.90%]	$\pm 20 \text{ cm}$ [57.97%]
std	± 5.74	± 10.27	± 5.51	± 10.91	± 5.31	± 10.69	± 5.78	± 10.27
mean	-2.20	-5.15	-1.38	-3.84	-1.41	-4.04	-2.13	-5.16
rms	± 6.15	± 11.49	± 5.68	± 11.57	± 5.50	± 11.43	± 6.17	± 11.49

Ellipsoidal height prediction at BMs

Dh $\leq \pm 20$ cm (left) and Dh $\geq \pm 20$ cm (right)



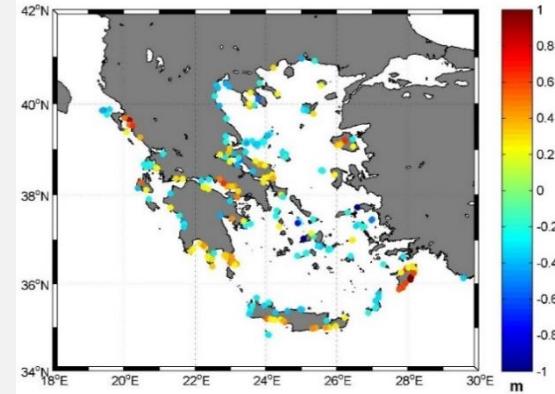
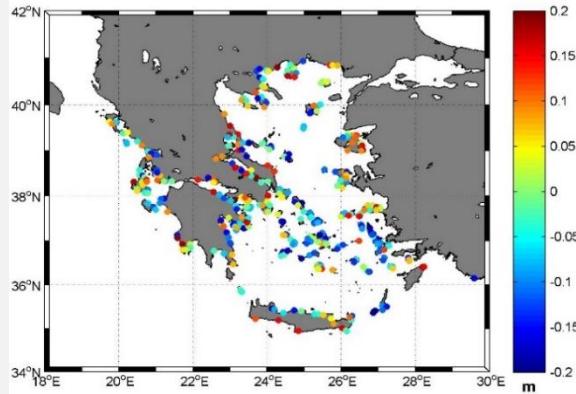
Exponential model [420/602]



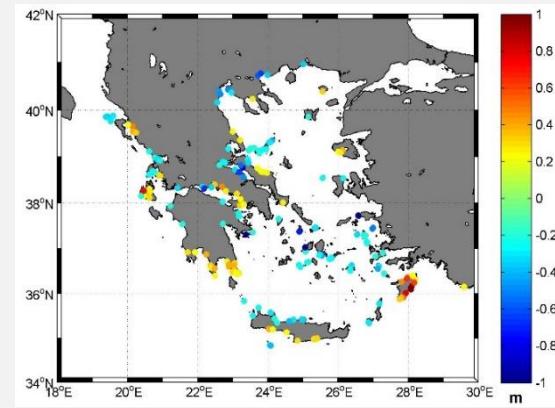
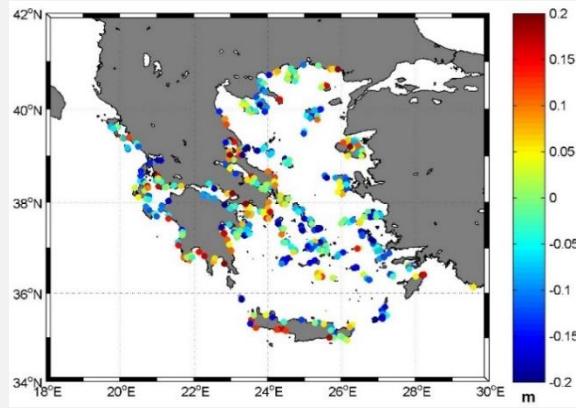
3rd order polynomial model [376/602]

Ellipsoidal height prediction at BMs

Dh $\leq \pm 20$ cm (left) and Dh $\geq \pm 20$ cm (right)



4th order polynomial model [376/602]

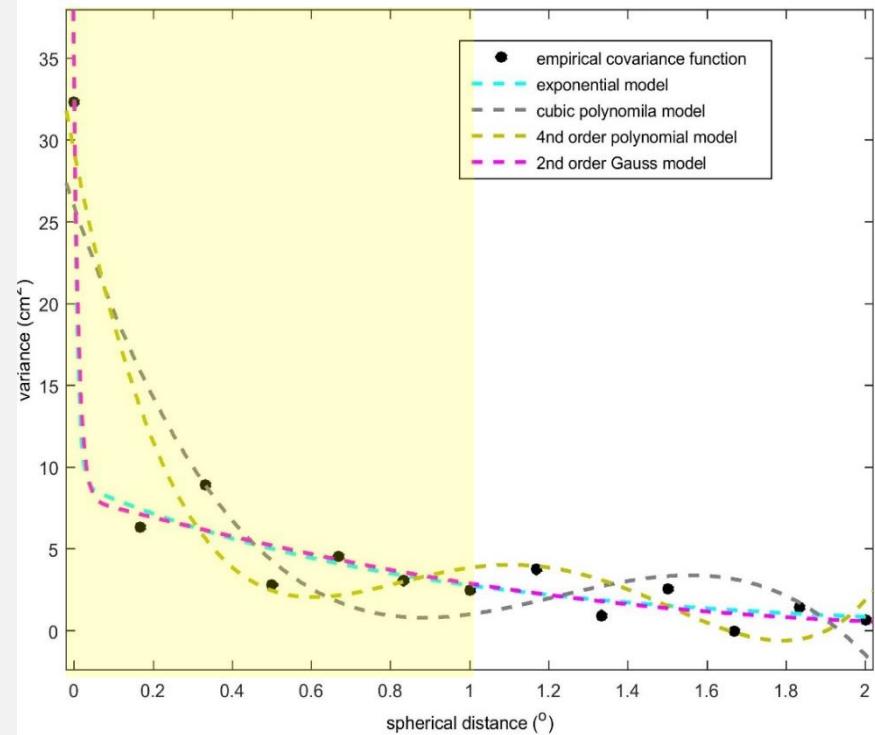
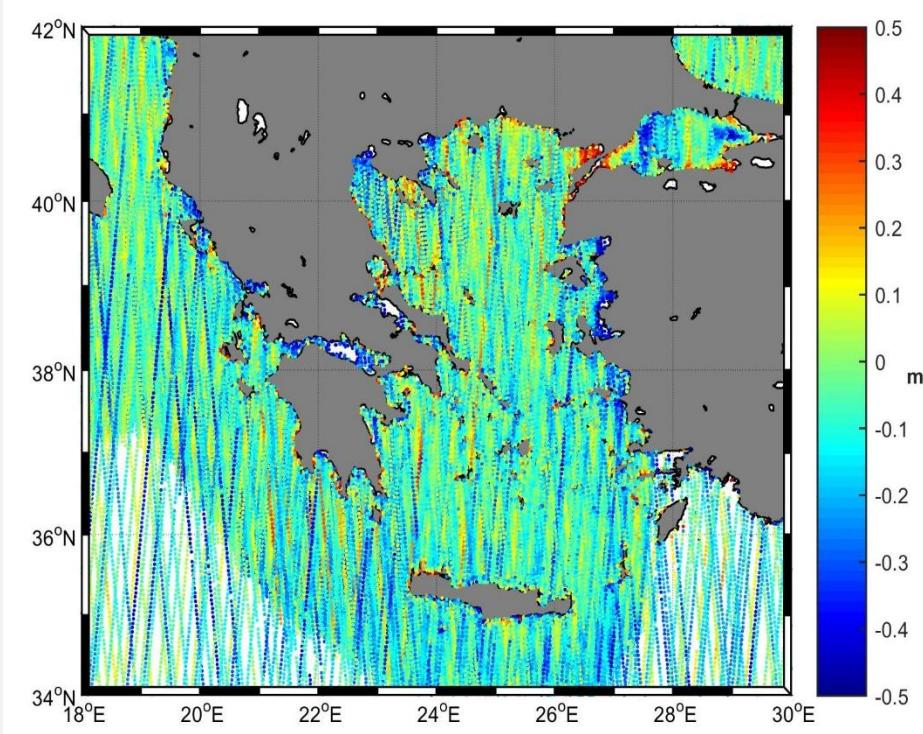


4th order Gauss model [420/602]

no correlation between prediction accuracy and topography

Ellipsoidal height prediction at BMs

Least Squares Collocation – Irregular data



Ellipsoidal height prediction at BMs

Least Squares Collocation – Irregular data

Remove Local Vertical Offset : -74.26 cm

[cm]	Exponential model [532/602]	3rd order polynomial model [197/602]	4th order polynomial model [353/602]	2nd order Gauss model [431/602]
std	±22.54	±76.28	±66.31	±23.95
mean	-76.49	-74.7	-25.21	-44.14
	±10 cm [35.88%]	±20 cm [61.46%]	±10 cm [3.65%]	±20 cm [6.81%]
std	±5.58	±10.55	±6.11	±11.42
mean	-0.48	-2.20	-1.38	-1.25
rms	±5.60	±10.78	±6.26	±11.49

Remove Local Vertical Offset : -64.91 cm

[cm]	Exponential model [532/602]	3rd order polynomial model [197/602]	4th order polynomial model [353/602]	2nd order Gauss model [431/602]
	±10 cm [26.08%]	±20 cm [51.50%]	±10 cm [2.32%]	±20 cm [7.48%]
std	±5.65	10.52	±5.78	±10.85
mean	-1.92	-4.62	-1.65	-3.74
rms	±5.97	11.49	±6.01	±11.47

Ellipsoidal height prediction at BMs

Least Squares Collocation – Irregular vs. gridded data

Remove Local Vertical Offset : -74.26 cm

[cm]	Exponential model [532/602]		Exponential model (gridded)	
std	± 22.54		± 23.45	
mean	-76.49		-77.63	
	± 10 cm [35.88%]	± 20 cm [61.46%]	± 10 cm [42.03%]	± 20 cm [69.77%]
std	± 5.58	± 10.55	± 5.47	± 10.18
mean	-0.48	-2.20	-0.59	-2.56
rms	± 5.60	± 10.78	± 5.50	± 10.50

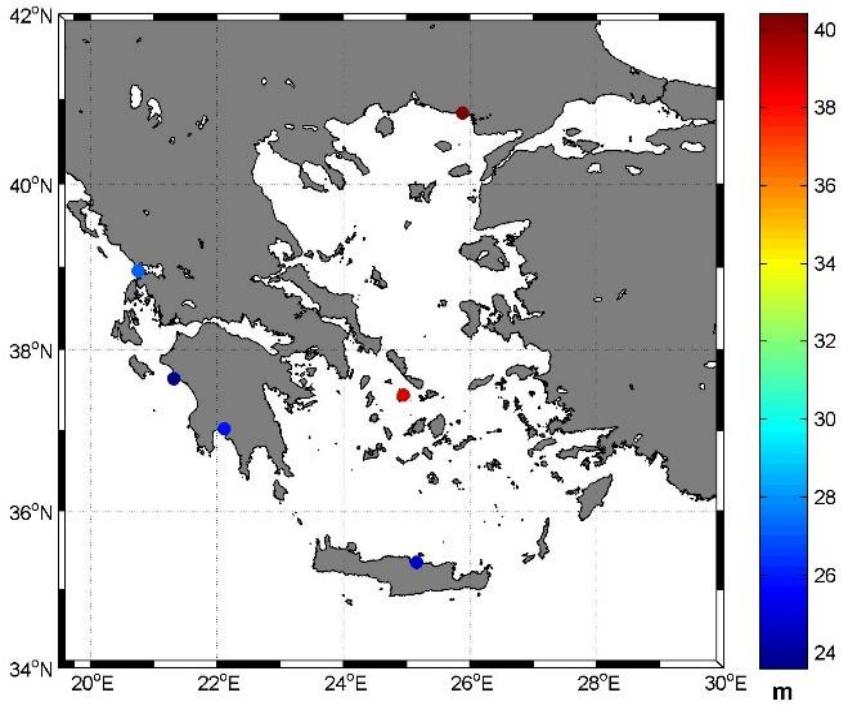
Remove Local Vertical Offset : -64.91 cm

[cm]	Exponential model [532/602]		Exponential model (gridded)	
	± 10 cm [26.08%]	± 20 cm [51.50%]	± 10 cm [29.73%]	± 20 cm [57.97%]
std	± 5.65	10.52	± 5.74	± 10.27
mean	-1.92	-4.62	-2.20	-5.15
rms	± 5.97	11.49	± 6.15	± 11.49

Ellipsoidal height prediction at TGs

Tide gauges in Greece (SONEL)

$$\hat{h} = \text{MSS} + \text{SLA}$$



PSMSL ID	Latitude(°)	Longitude(°)	Station
1238	40.84414	25.87827	ALEXANDROUPOLIS
634	35.34848	25.15269	IRAKLION
411	37.02368	22.11584	KALAMAI
1240	37.64482	21.31968	KATAKOLON
410	38.95908	20.75663	PREVEZA
1234	37.43997	24.94581	SIROS

PSMSL ID	Ellipsoidal Heights [m]	
	Tide free system	Mean tide system
1238	40.419	40.402
634	24.705	24.705
411	25.761	25.756
1240	23.607	23.600
410	27.055	27.044
1234	38.634	38.628

Altimetric data -> mean tide system

Tide gauges data -> tide free system

$$h^{\text{MT}} = h^{\text{TF}} + 0.62 \left(0.099 - 0.296 \sin^2 \varphi \right)$$

Ellipsoidal height prediction at TGs

Cubic interpolation – Gridded data (CASE E)

PSML ID	[unit: m]					LVD (-74.26 cm)		LVD (-64.91 cm)	
	h_{INITIAL}	DTU13 MSS	SLA	$h_{\text{INITIAL}} - \text{MSS}$	$h_{\text{INITIAL}} - (\text{MSS} + \text{SLA})$	$h_{\text{INITIAL}} - \text{MSS}$	$h_{\text{INITIAL}} - (\text{MSS} + \text{SLA})$	$h_{\text{INITIAL}} - \text{MSS}$	$h_{\text{INITIAL}} - (\text{MSS} + \text{SLA})$
1238	40.402	40.869	-0.005	-0.467	-0.462	0.276	0.281	0.182	0.187
634	24.705	25.29	0.081	-0.585	-0.666	0.158	0.077	0.064	-0.017
411	25.756	26.441	0.091	-0.685	-0.775	0.058	-0.032	-0.036	-0.126
1240	23.600	24.275	0.033	-0.675	-0.708	0.068	0.035	-0.026	-0.059
410	27.044	27.872	-0.139	-0.828	-0.689	-0.085	0.054	-0.179	-0.04
1234	38.628	39.296	0.05	-0.668	-0.719	0.075	0.024	-0.019	-0.07
Statistics	min	-0.828	-0.775		-0.058	0.024		-0.179	-0.126
	max	-0.467	-0.462		0.158	0.281		0.182	0.187
	std	±0.120	±0.108		±0.120	±0.108		±0.120	±0.108
	mean	-0.651	-0.67		0.091	0.073		-0.002	-0.021
	rms	±0.662	±0.678		±0.150	±0.130		±0.120	±0.110

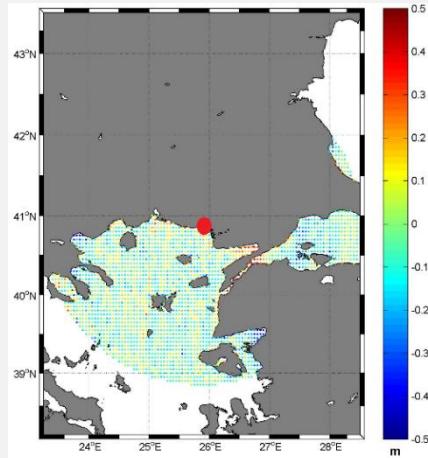
Ellipsoidal height prediction at TGs

Cubic interpolation – Gridded data (CASE E)

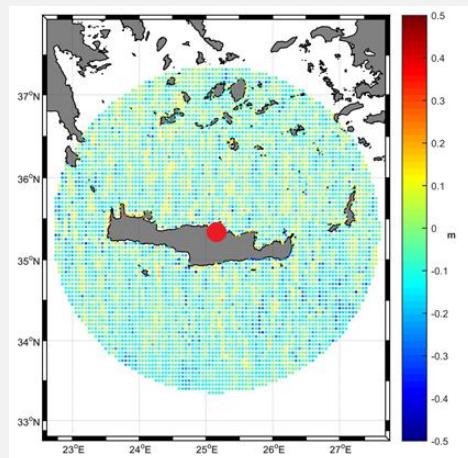
PSML ID	[unit: m]					LVD (-74.26 cm)		LVD (-64.91 cm)	
	h_{INITIAL}	DTU13 MSS	SLA	$h_{\text{INITIAL}} - \text{MSS}$	$h_{\text{INITIAL}} - (\text{MSS} + \text{SLA})$	$h_{\text{INITIAL}} - \text{MSS}$	$h_{\text{INITIAL}} - (\text{MSS} + \text{SLA})$	$h_{\text{INITIAL}} - \text{MSS}$	$h_{\text{INITIAL}} - (\text{MSS} + \text{SLA})$
1238	40.402	40.869	-0.005	-0.467	-0.462	0.276	0.281	0.182	0.187
634	24.705	25.29	0.081	-0.585	-0.666	0.158	0.077	0.064	-0.017
411	25.756	26.441	0.091	-0.685	-0.775	0.058	-0.032	-0.036	-0.126
1240	23.600	24.275	0.033	-0.675	-0.708	0.068	0.035	-0.026	-0.059
410	27.044	27.872	-0.139	-0.828	-0.689	-0.085	0.054	-0.179	-0.04
1234	38.628	39.296	0.05	-0.668	-0.719	0.075	0.024	-0.019	-0.07
Statistics	min	-0.828	-0.775		-0.085	-0.032		-0.179	-0.126
	max	-0.585	-0.666		0.158	0.077		0.064	-0.017
	std	±0.088	±0.041		±0.088	±0.041		±0.088	±0.041
	mean	-0.688	-0.711		0.055	0.032		-0.039	-0.062
	rms	0.694	0.713		±0.103	±0.052		±0.096	±0.075

Ellipsoidal height prediction at TGs

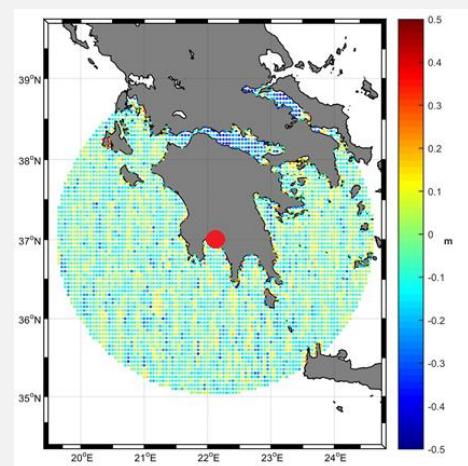
Least Squares Collocation – Gridded data (CASE E), radius 2°



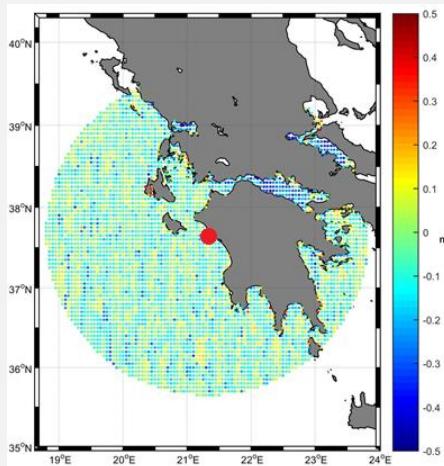
ALEXANDROUPOLIS



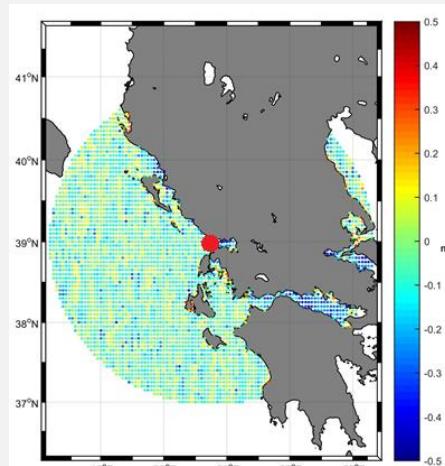
IRAKLION



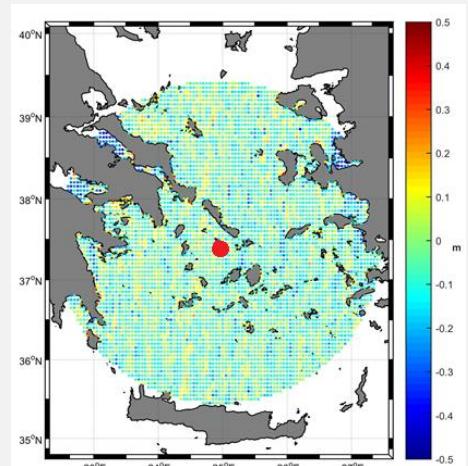
KALAMAI



KATAKOLON



PREVEZA



SIROS

Ellipsoidal height prediction at TGs

Least Squares Collocation – Gridded data (CASE E), radius 2°

PSMSL	Exponential model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	2.44E-05	-0.467	0.276	0.182	
634	1.22E-02	-0.597	0.145	0.052	
411	5.32E-05	-0.685	0.058	-0.036	
1240	1.31E-03	-0.676	0.066	-0.027	
410	-1.84E-04	-0.828	-0.085	-0.179	
1234	1.63E-03	-0.670	0.073	-0.021	
min		-0.828	-0.085	-0.179	
max		-0.467	0.276	0.182	
std		±0.118	±0.118	±0.118	
mean		-0.654	0.089	-0.005	
rms		±0.664	±0.148	±0.119	

PSMSL	4th order Gauss model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	2.23E-14	-0.467	0.276	0.182	
634	1.07E-02	-0.596	0.147	0.053	
411	-2.63E-10	-0.685	0.058	-0.036	
1240	1.40E-04	-0.675	0.067	-0.026	
410	-1.90E-10	-0.828	-0.085	-0.179	
1234	2.08E-03	-0.670	0.073	-0.021	
min		-0.828	-0.085	-0.179	
max		-0.467	0.276	0.182	
std		±0.119	±0.119	±0.119	
mean		-0.653	0.089	-0.004	
rms		±0.664	±0.148	±0.119	

Ellipsoidal height prediction at TGs

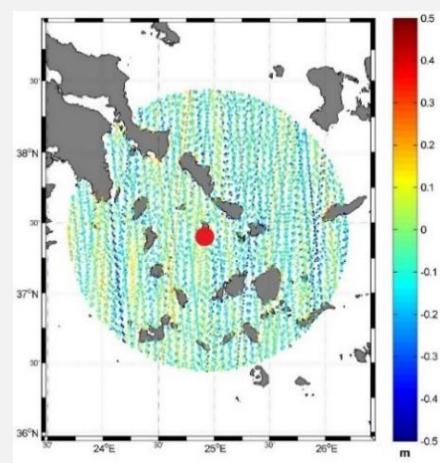
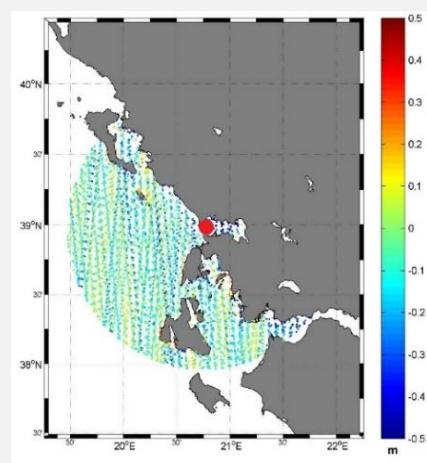
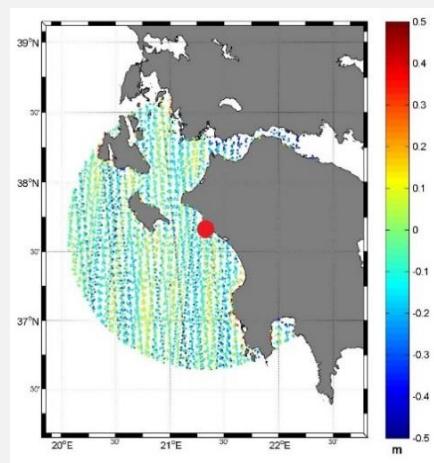
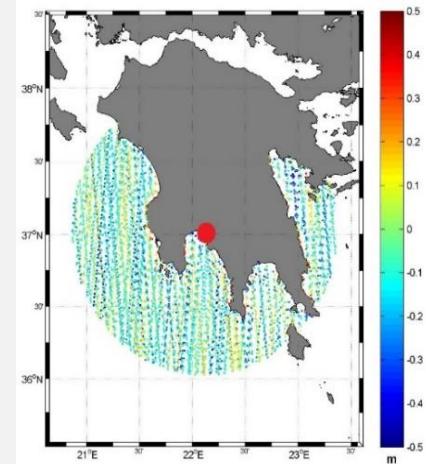
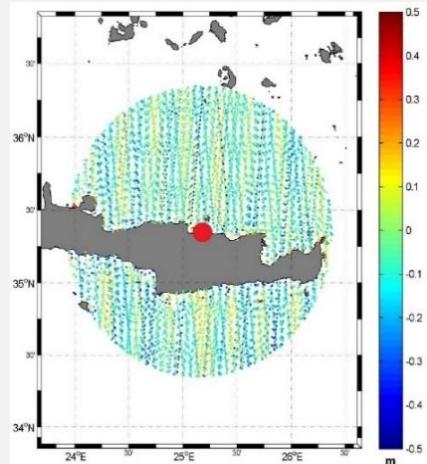
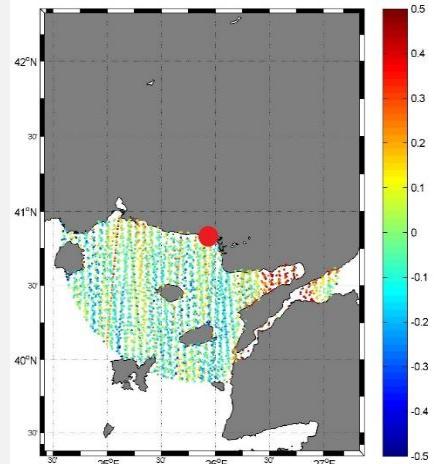
Least Squares Collocation – Gridded data (CASE E), radius 2°

PSMSL	3rd order polynomial model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	0.077	-0.544	0.198	0.105	
634	0.086	-0.671	0.072	-0.022	
411	0.128	-0.813	-0.071	-0.164	
1240	0.056	-0.731	0.012	-0.082	
410	-0.140	-0.688	0.055	-0.039	
1234	0.100	-0.768	-0.025	-0.119	
min		-0.813	-0.071	-0.164	
max		-0.544	0.198	0.105	
std		±0.093	±0.093	±0.093	
mean		-0.702	0.040	-0.053	
rms		±0.709	±0.102	±0.108	

PSMSL	4th order polynomial model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	0.093	-0.560	0.182	0.089	
634	0.081	-0.666	0.077	-0.017	
411	0.121	-0.806	-0.063	-0.157	
1240	0.055	-0.730	0.012	-0.081	
410	-0.137	-0.691	0.051	-0.042	
1234	0.088	-0.756	-0.014	-0.107	
min		-0.806	-0.063	-0.157	
max		-0.560	0.182	0.089	
std		±0.085	±0.085	±0.085	
mean		-0.702	0.041	-0.053	
rms		±0.707	±0.094	±0.100	

Ellipsoidal height prediction at TGs

Least Squares Collocation – Irregular data, radius 1°



Ellipsoidal height prediction at TGs

Least Squares Collocation – Irregular data, radius 1°

PSMSL	Exponential model [unit: m]					PSMSL	2nd order Gauss model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm		ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	-	-	-	-	-	1238	-	-	-	-	-
634	-	-	-	-	-	634	-	-	-	-	-
411	-2.04E-04	-0.685	0.058	-0.036		411	-6.58E-08	-0.685	0.058	-0.036	
1240	-8.27E-03	-0.667	0.076	-0.018		1240	-6.22E-03	-0.669	0.074	-0.020	
410	-4.34E-04	-0.828	-0.085	-0.178		410	-1.14E-05	-0.828	-0.085	-0.179	
1234	-	-	-	-	-	1234	-	-	-	-	-
min		-0.828	-0.085	-0.178		min		-0.828	-0.085	-0.179	
max		-0.667	0.076	-0.018		max		-0.669	0.074	-0.020	
std		±0.088	±0.088	±0.088		std		±0.088	±0.088	±0.088	
mean		-0.726	0.016	-0.077		mean		-0.727	0.015	-0.078	
rms		±0.732	±0.090	±0.117		rms		±0.733	±0.089	±0.117	

Ellipsoidal height prediction at TGs

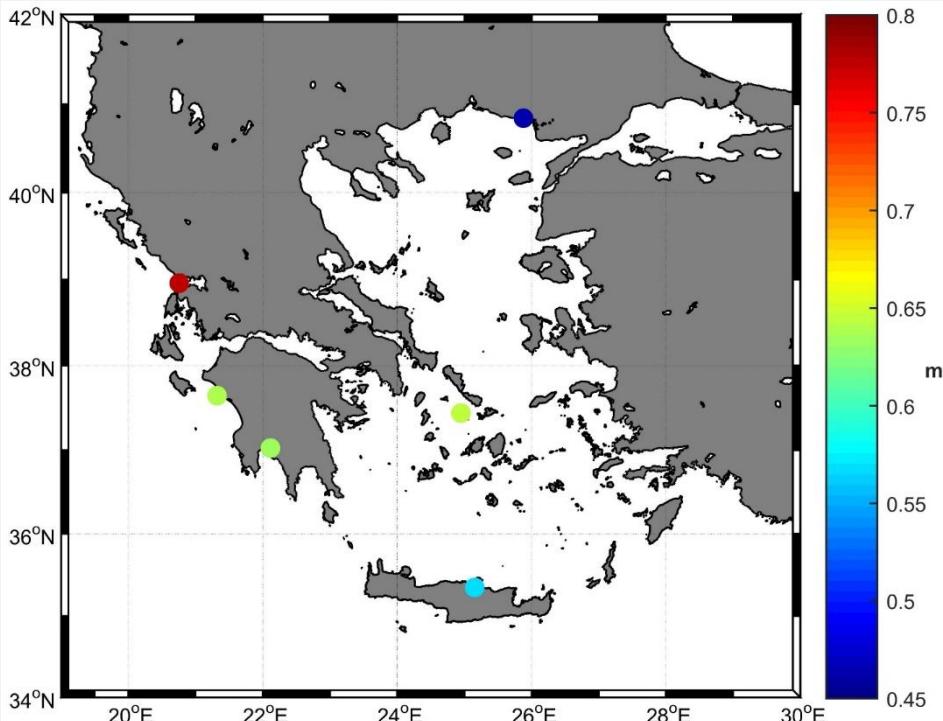
Least Squares Collocation – Irregular vs. gridded data

PSMSL	Exponential model (irregular) [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	-	-	-	-	-
634	-	-	-	-	-
411	-2.04E-04	-0.685	0.058	-0.036	
1240	-8.27E-03	-0.667	0.076	-0.018	
410	-4.34E-04	-0.828	-0.085	-0.178	
1234	-	-	-	-	-
<hr/>					
min		-0.828	-0.085	-0.178	
max		-0.667	0.076	-0.018	
std		±0.088	±0.088	±0.088	
mean		-0.726	0.016	-0.077	
rms		±0.732	±0.090	±0.117	

PSMSL	4th order polynomial model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	0.093	-0.560	0.182	0.089	
634	0.081	-0.666	0.077	-0.017	
411	0.121	-0.806	-0.063	-0.157	
1240	0.055	-0.730	0.012	-0.081	
410	-0.137	-0.691	0.051	-0.042	
1234	0.088	-0.756	-0.014	-0.107	
<hr/>					
min		-0.806	-0.063	-0.157	
max		-0.560	0.182	0.089	
std		±0.085	±0.085	±0.085	
mean		-0.702	0.041	-0.053	
rms		±0.707	±0.094	±0.100	

Time-series construction/analysis

Local vertical offsets of TGs



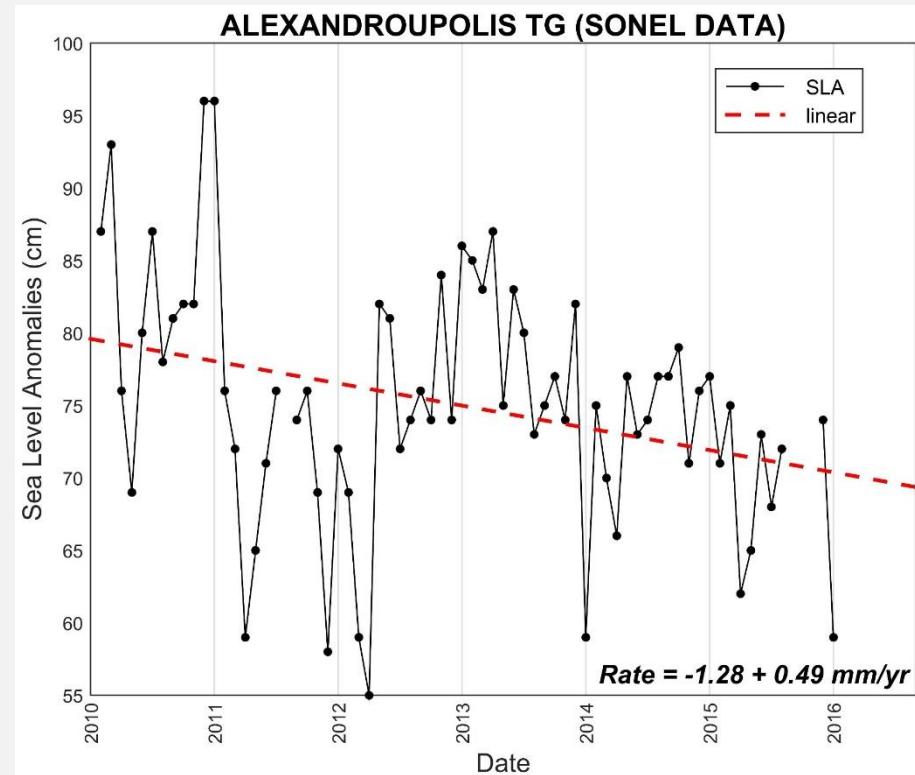
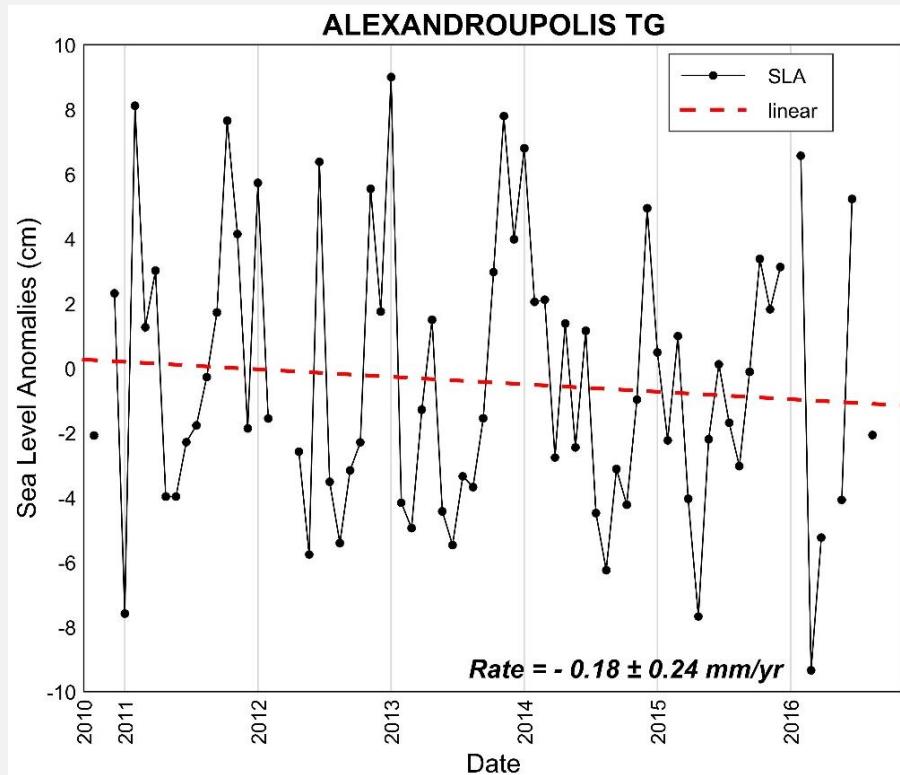
Cubic interpolation per cycle

- ✓ Gridded along track SLA data
- ✓ 2D low pass filtering
- ✓ prediction at BMs

$$\text{LVO} = h_{\text{initial}} - h_{\text{estimated}}$$

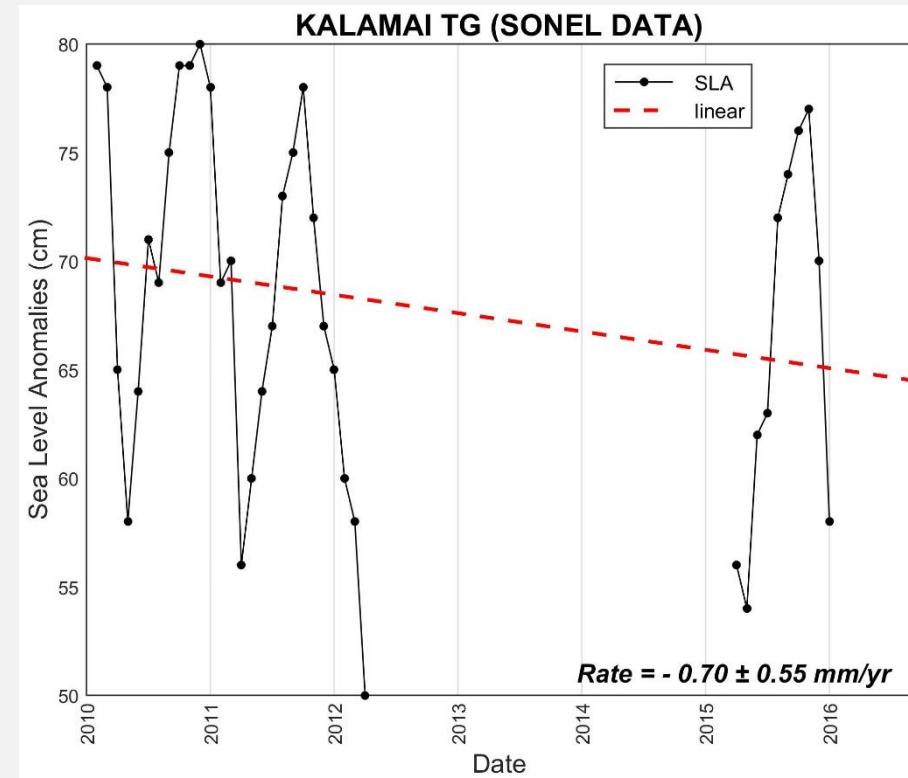
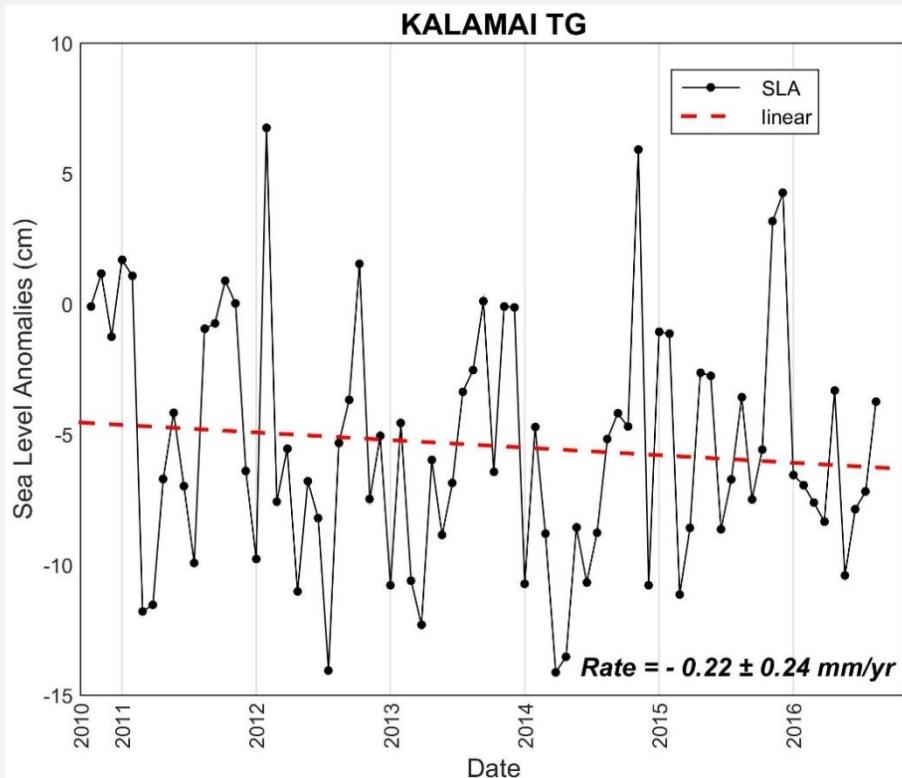
Time-series construction/analysis

TGs check points



Time-series construction/analysis

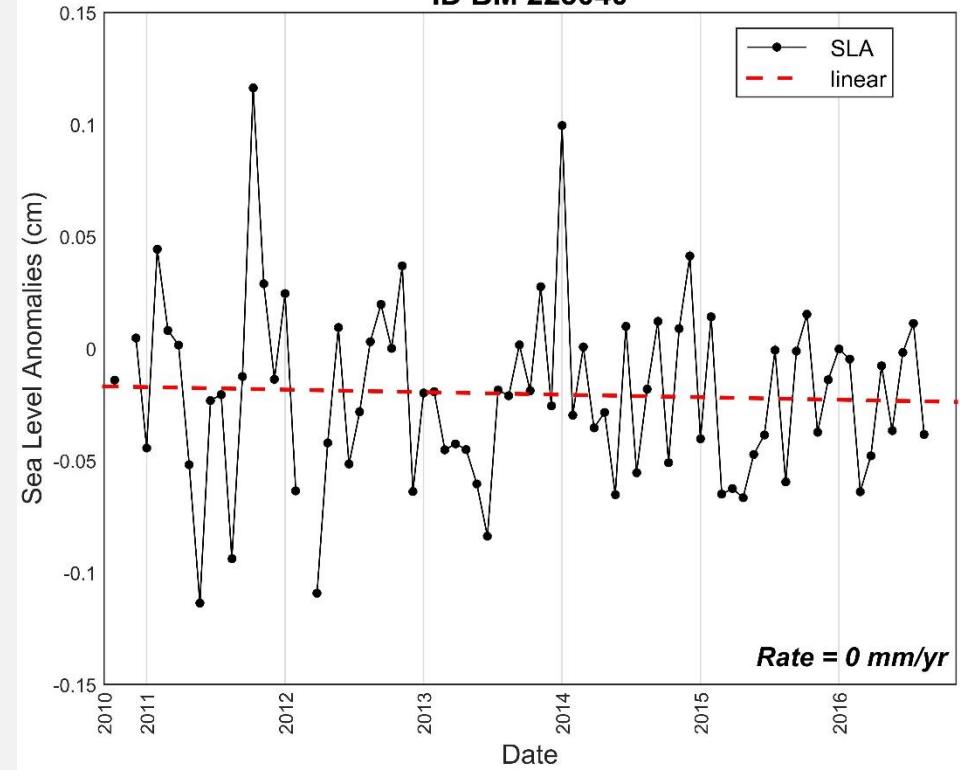
TGs check points



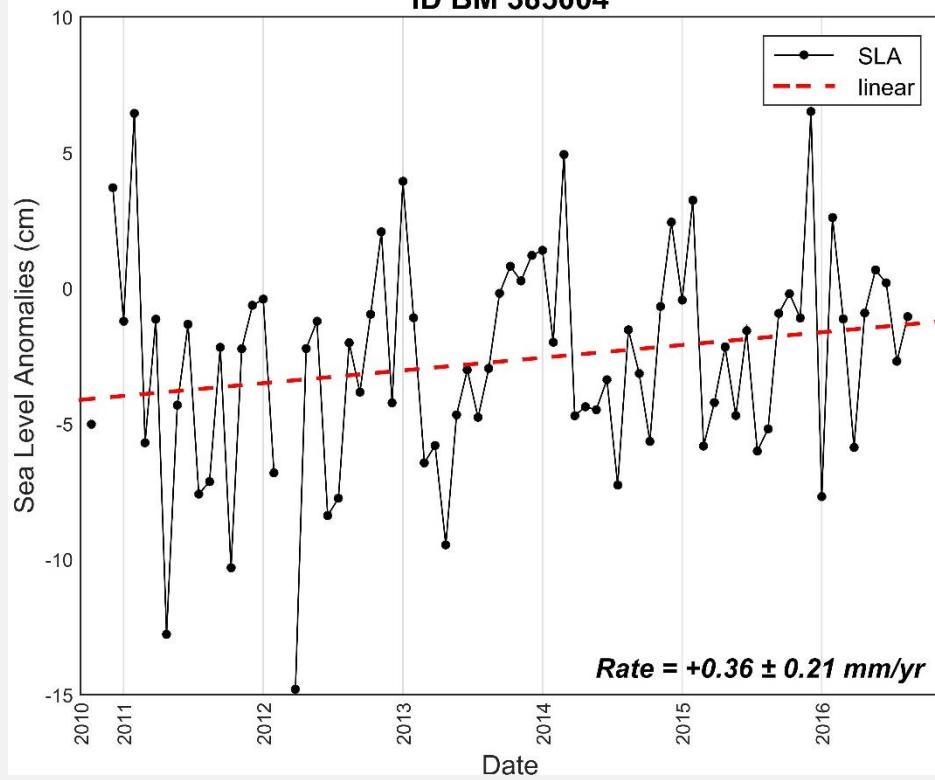
Time-series construction/analysis

BMs check points

ID BM 223040



ID BM 385004



Time-series construction/analysis

Local vertical offsets

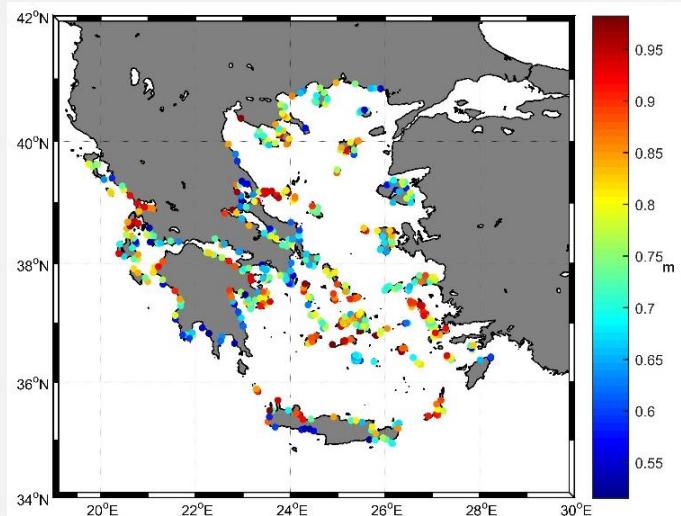
(Jason ellipsoid, MT and IAG W_o)

$$\delta\widehat{W}_o^{Gr\ LVD} = -66.84 \text{ cm}$$

TGs check points

6 TGs -> -62.00 cm

4 TGs -> -62.04 cm (except ALEXANDROUPOLIS and PREVEZA)



BMs check points

602 BM -> -74.95 cm

1σ test (std=23.5 cm) -> 465 BMs, new offset -> -76.47 cm

Time-series construction/analysis

Local vertical offsets

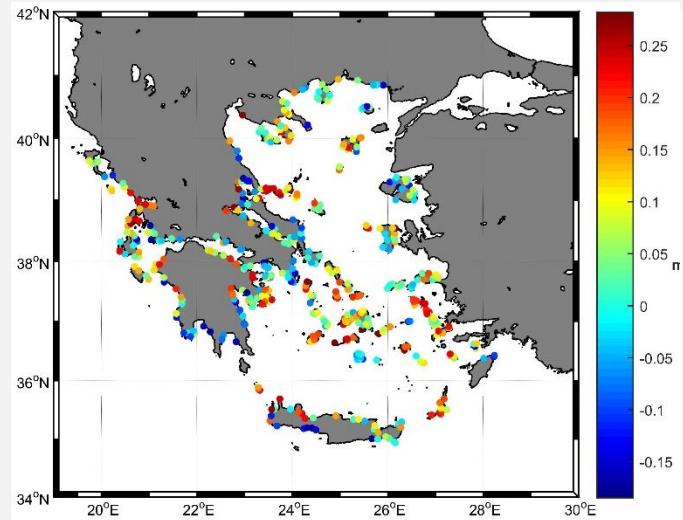
(GRS80 ellipsoid, MT and IAG W_o)

$$\delta\widehat{W}_o^{Gr\ LVD} = +3.16 \text{ cm}$$

TGs check points

6 TGs -> +8.00 cm

4 TGs -> +8.04 cm (except ALEXANDROUPOLIS and PREVEZA)



BMs check points

602 BM -> -4.95 cm

1σ test (std=23.5 cm) -> 465 BMs, new offset -> -6.47 cm

Conclusions

- No-bias during alternation of altimeter modes (LRM, SAR, SARIN)
- RDSAR → high observation noise (std > ±10 cm)
- SAR/SARin → new information closer to the coast – high observation noise
- Remove SSB – altimetry data need to be corrected

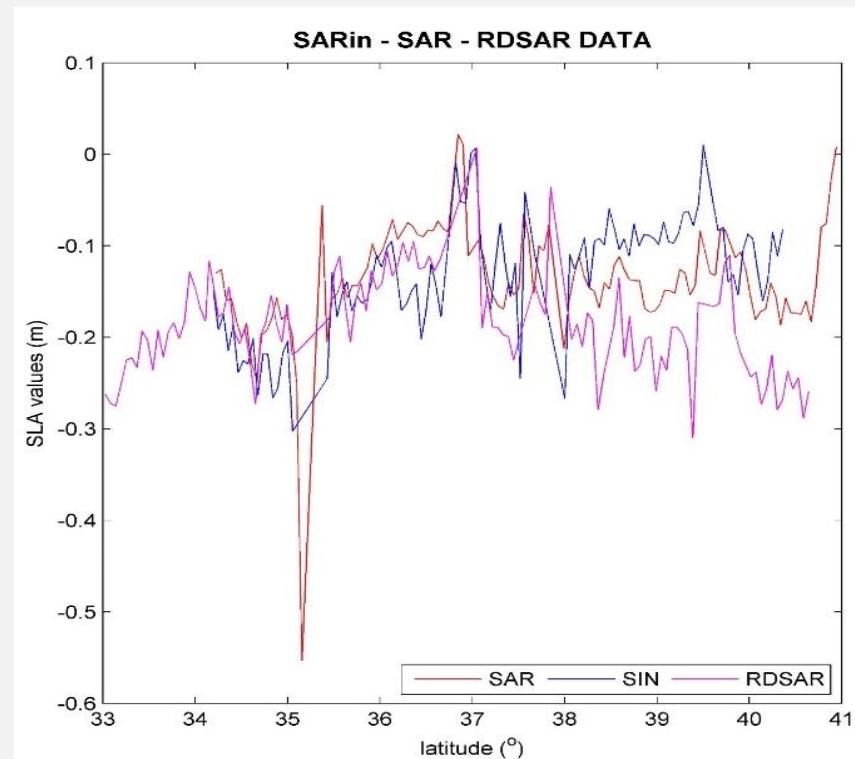
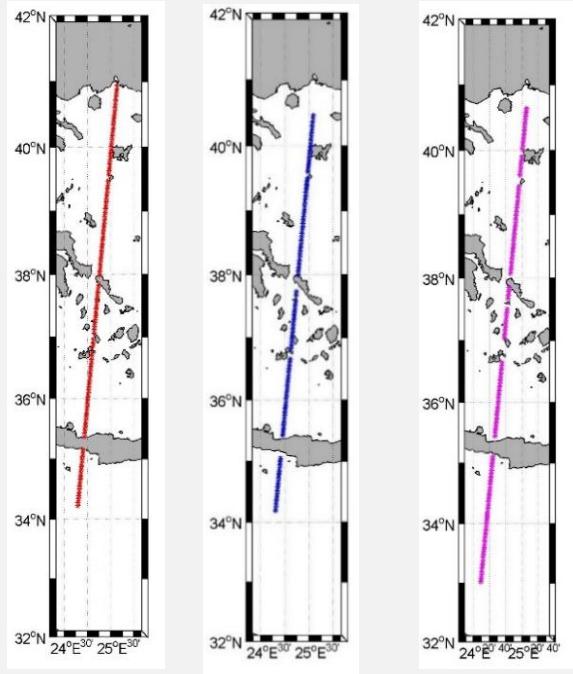
Conclusions

- Cubic interpolation – LSC (exponential and Gauss 4th order models)
- Data : 2D low pass filtering on grid
- Prediction accuracy ≈ 5 cm, $\Delta h < \pm 10$ cm for more than $\frac{1}{2}$ BMs
- 4-8 cm accuracy in the $\widehat{\delta W}_o^{Gr\ LVD}$ compared to the best estimate for the Greek LVD. Looks promising!
- Calculation of LVD Offset (602 BMs) : -4.95 cm (GRS80, MT)
- Little or no correlation between topography and prediction accuracy
- LSC: prediction accuracy is related to distance from prediction point and quality of altimetric observations

Back-up slides

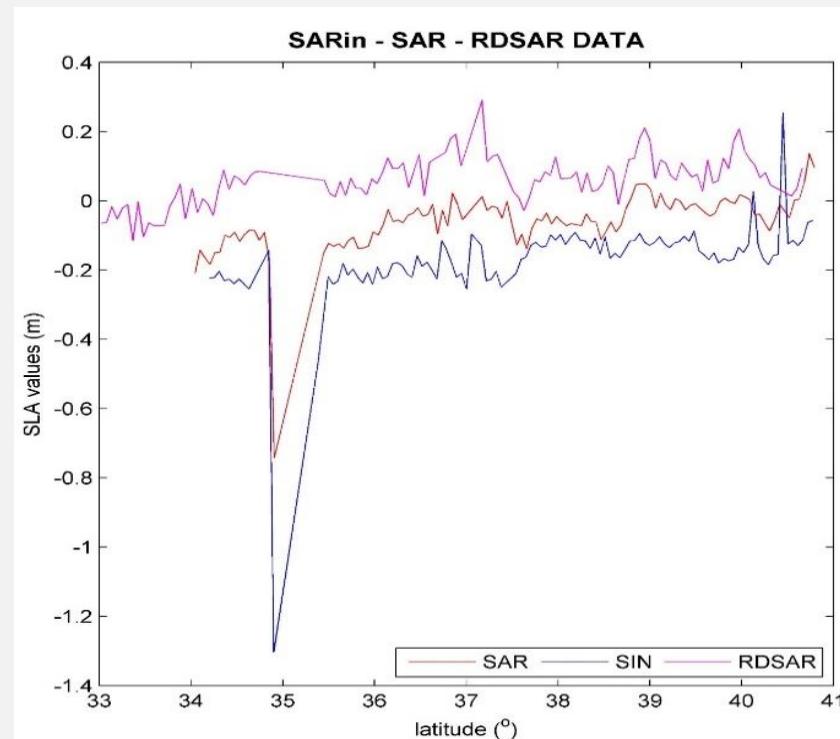
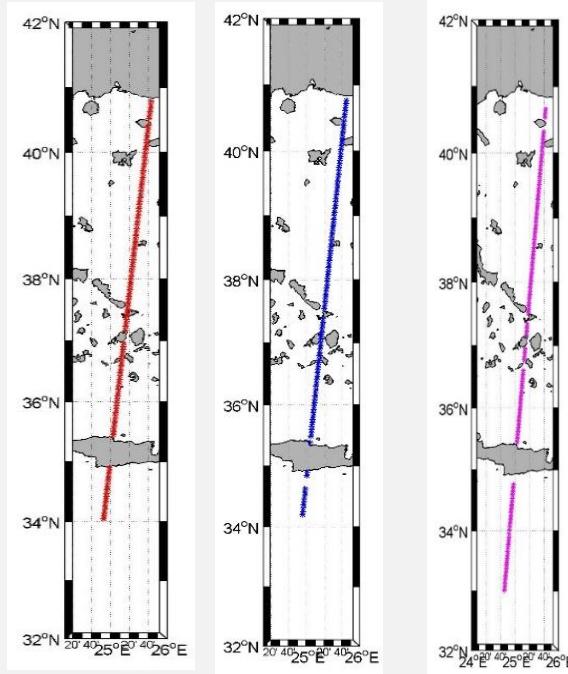
Evaluation of SAR – SARin – RDSAR data in Greece

February : cycle 37 (SAR, RDSAR) - cycle 76 (SARin)



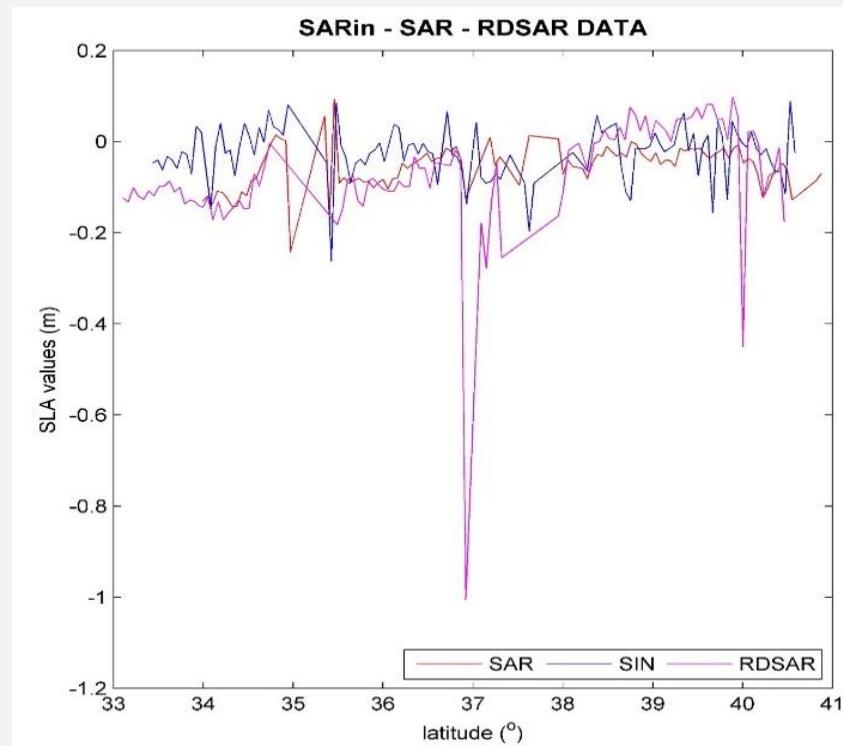
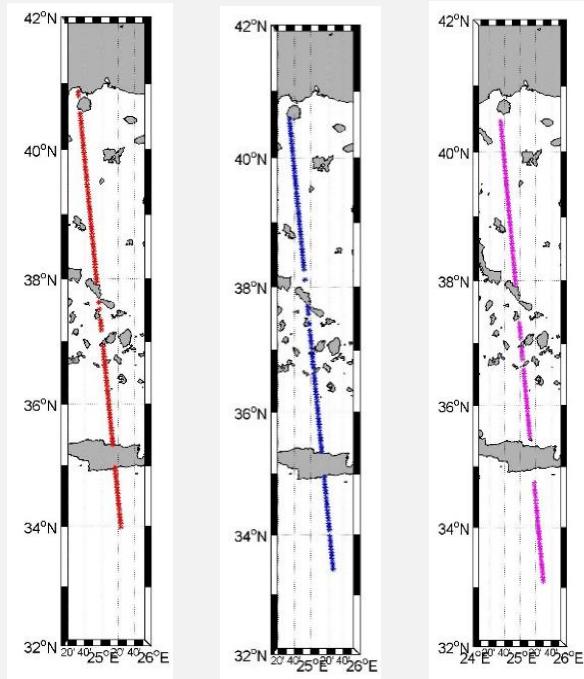
Evaluation of SAR – SARin – RDSAR data in Greek region

March : cycle 38 (SAR, RDSAR) - cycle 77 (SARin)



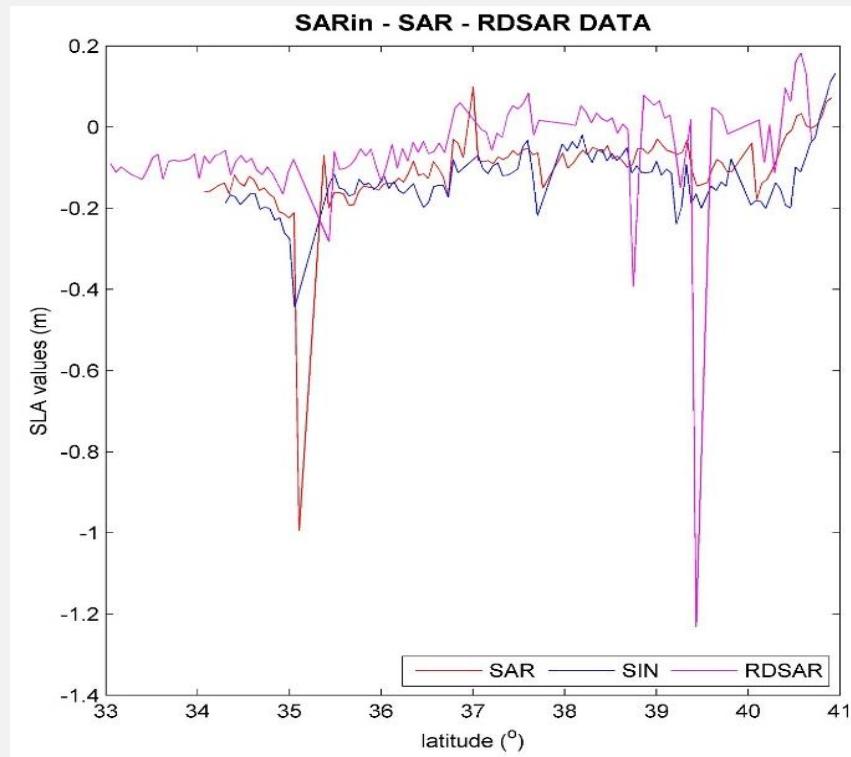
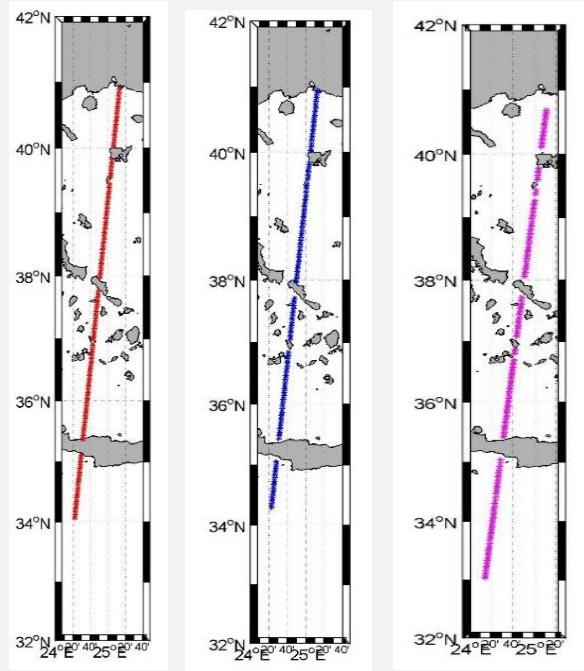
Evaluation of SAR – SARin – RDSAR data in Greek region

April : cycle 39 (SAR, RDSAR) - cycle 78 (SARin)



Evaluation of SAR – SARin – RDSAR data in Greek region

May : cycle 40 (SAR, RDSAR) - cycle 79 (SARin)



Ellipsoidal height prediction at TGs

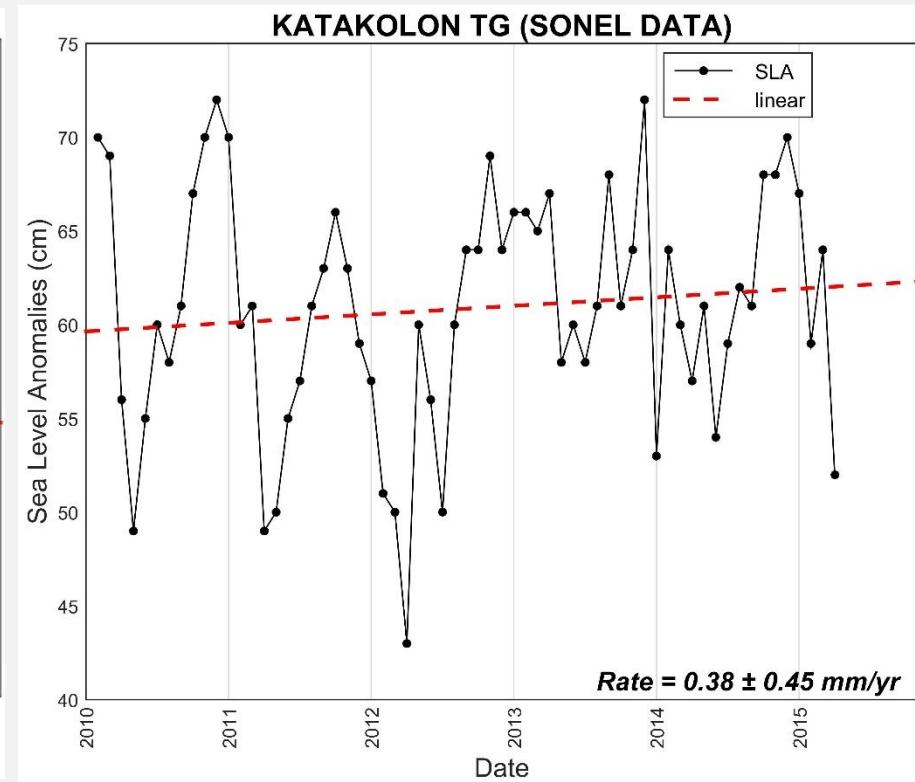
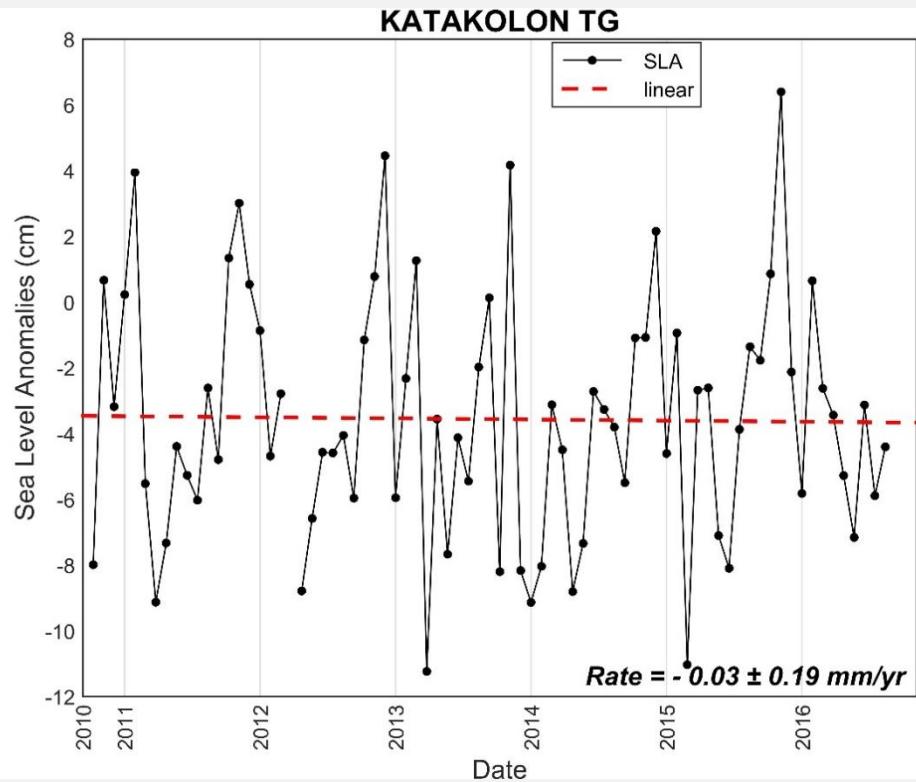
Least Squares Collocation – Irregular data, radius 1°

PSMSL	3rd order polynomial model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	-	-	-	-	-
634	-	-	-	-	-
411	0.309	-0.994	-0.252	-0.345	
1240	-1.472	0.797	1.540	1.446	
410	2.176	-3.004	-2.261	-2.355	
1234	-	-	-	-	-
min		-3.004	-2.261	-2.355	
max		0.797	1.540	1.446	
std		±1.902	±1.902	±1.902	
mean		-1.067	-0.324	-0.418	
rms		±2.180	±1.929	±1.947	

PSMSL	4th order polynomial model [unit: m]				
	ID	SLA	h-(MSS+SLA)	Remove LVD -74.26 cm	Remove LVD -64.91 cm
1238	-	-	-	-	-
634	-	-	-	-	-
411	-0.636	-0.049	0.694	0.600	
1240	-0.014	-0.661	0.081	-0.012	
410	0.508	-1.336	-0.594	-0.687	
1234	-	-	-	-	-
min		-1.336	-0.594	-0.687	
max		-0.049	0.694	0.600	
std		±0.644	±0.644	±0.644	
mean		-0.682	0.060	-0.033	
rms		±0.938	±0.647	±0.645	

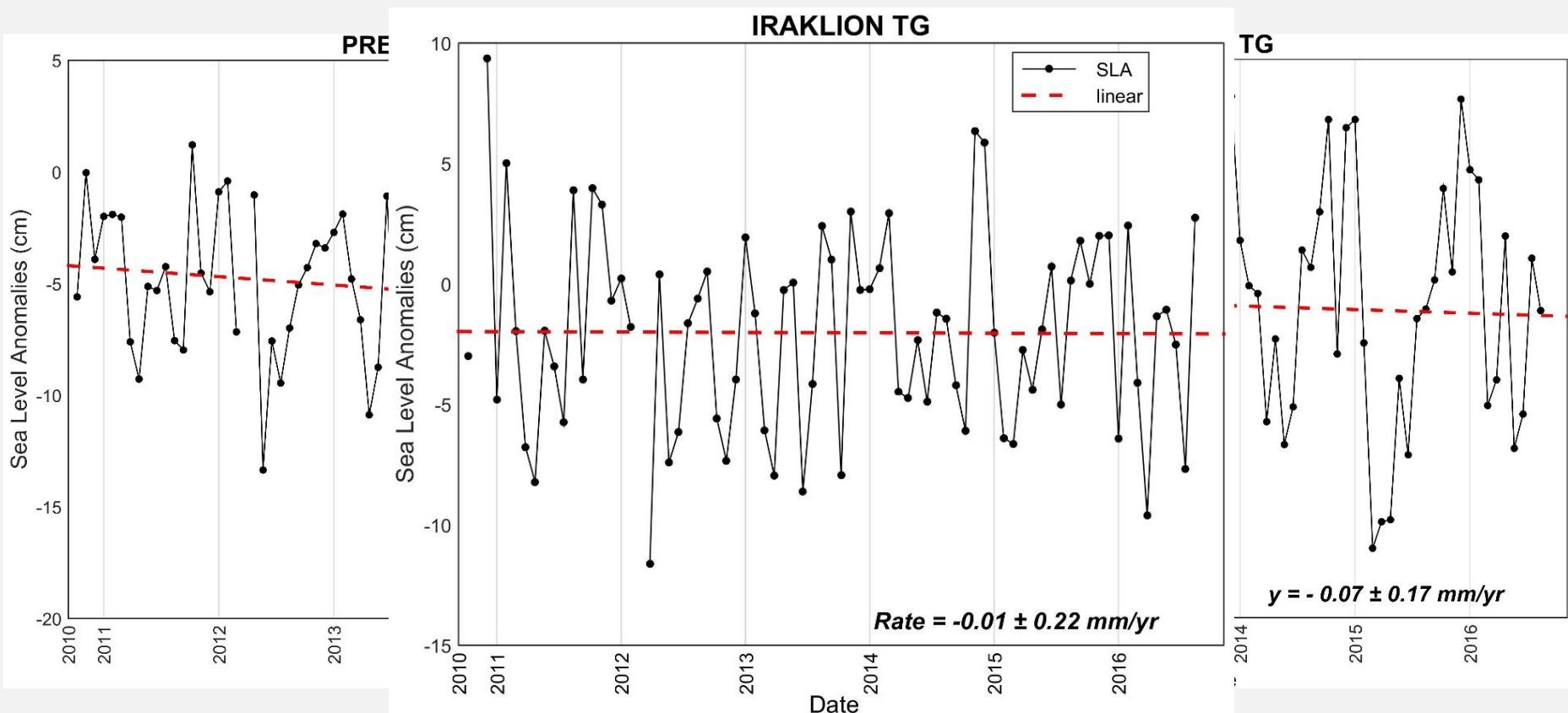
Time-series construction/analysis

TGs check points



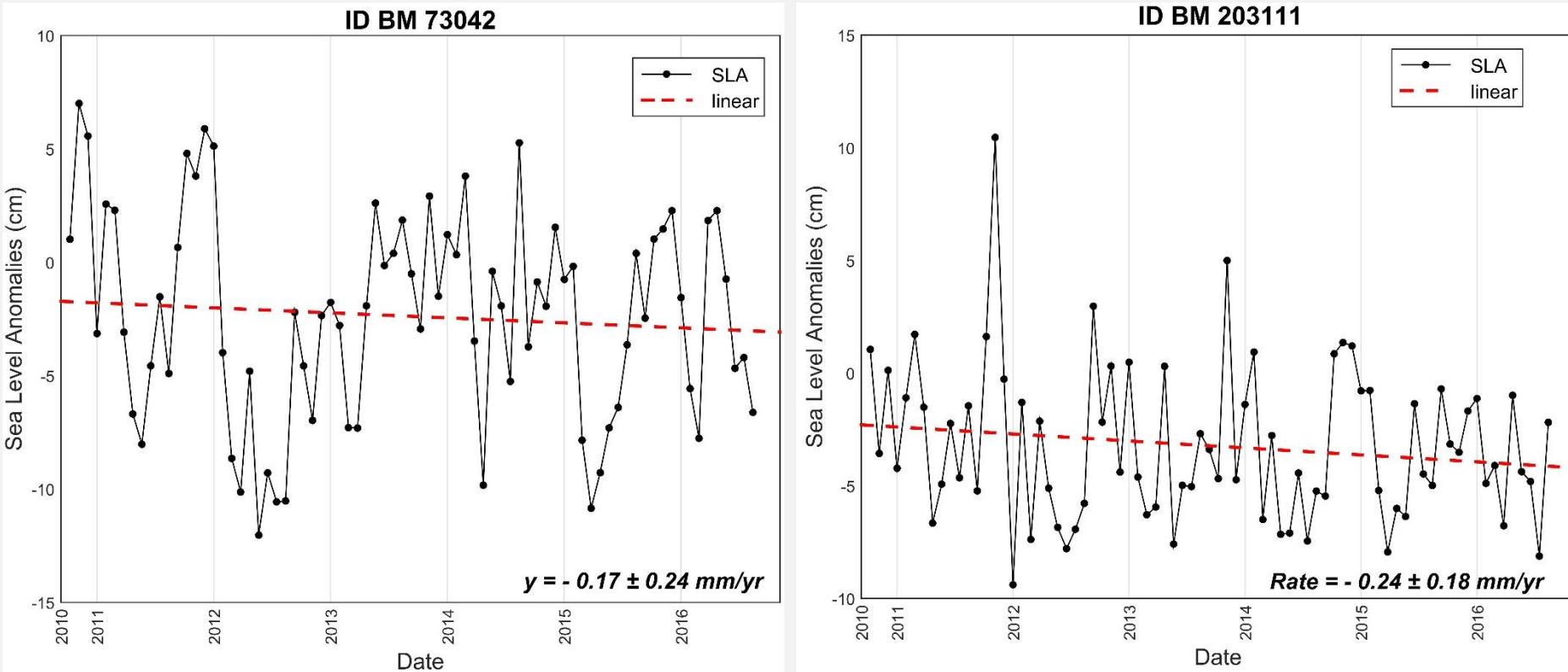
Time-series construction/analysis

TGs check points



Time-series construction/analysis

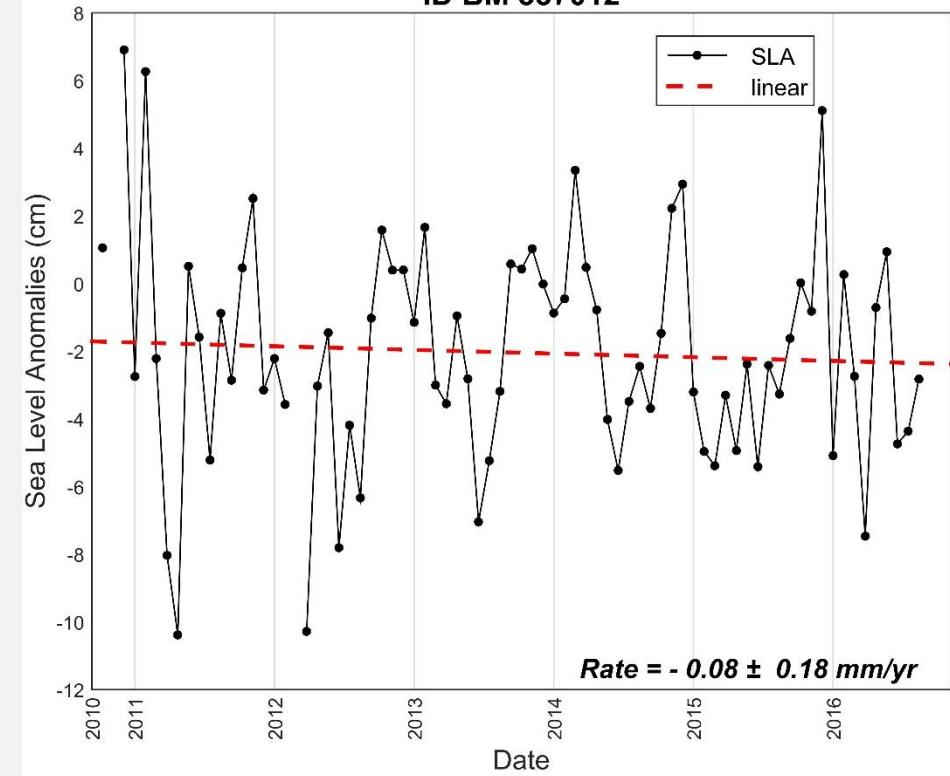
BMs check points



Time-series construction/analysis

BMs check points

ID BM 337012



ID BM 50023

