

**The GEOMED 2 project:
A high resolution geoid of the Mediterranean Sea**

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The GEOMED 2 project (1/2)

- The project aims at estimating the geoid over the area

$$30 < \varphi < 48 \quad -10 < \lambda < 40$$

with a resolution of 3'×3'

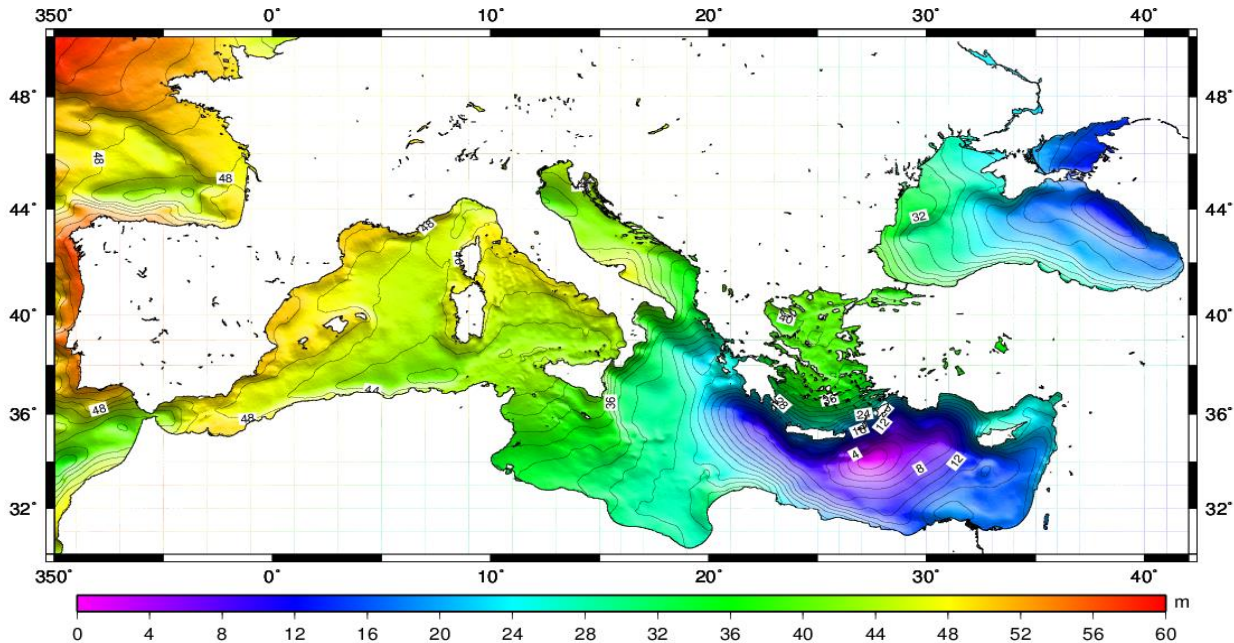
- ***Gravity data only will be used in the computation***

- Methods to be used in the geoid computation:

- i) Collocation
- ii) Stokes
- iii) Stokes-FFT

The GEOMED 2 project (2/2)

- DOT will be then computed by difference with existing MSS altimetry derived estimates (e.g. the DTU2013)



The DTU2013 MSS over the Mediterranean Sea

- The circulation in the Mediterranean Sea will be also estimated

The Adriatic Sea test

- The selected area

$$36 < \varphi < 48 \quad 10 < \lambda < 21$$

- Gravity data selected with a mean spacing of 2'x2' from the following databases:

- i) BGI
- ii) SHOM
- iii) Croatia
- iv) Greece
- v) Italy
- vi) EGM2008 (void areas along the Eastern edge)

- Geoid estimate based on the Remove-Restore method

- The DTM/bathymetry model is **SRTM/NOAA** bathymetry at 3''x3'' (bathymetry is originally at 1'x1') in the window

$$35 < \varphi < 49 \quad 9 < \lambda < 22$$

- The **GGN GOCE-DIR5** to d/o **230** was used for the long wavelength modelling of gravity/geoid
- RTC effect was computed using the **GRAVSOFT TC** program (r=80 km from each computation point, data point heights equal to DTM). The reference DTM was estimated by low-pass filtering the detailed DTM (using a 25' cap)
- Residual gravity values were gridded using the **GRAVSOFT GEOGRID** program on a regular 3'x3' geographical grid in the area

$$36 < \varphi < 48 \quad 10 < \lambda < 21$$

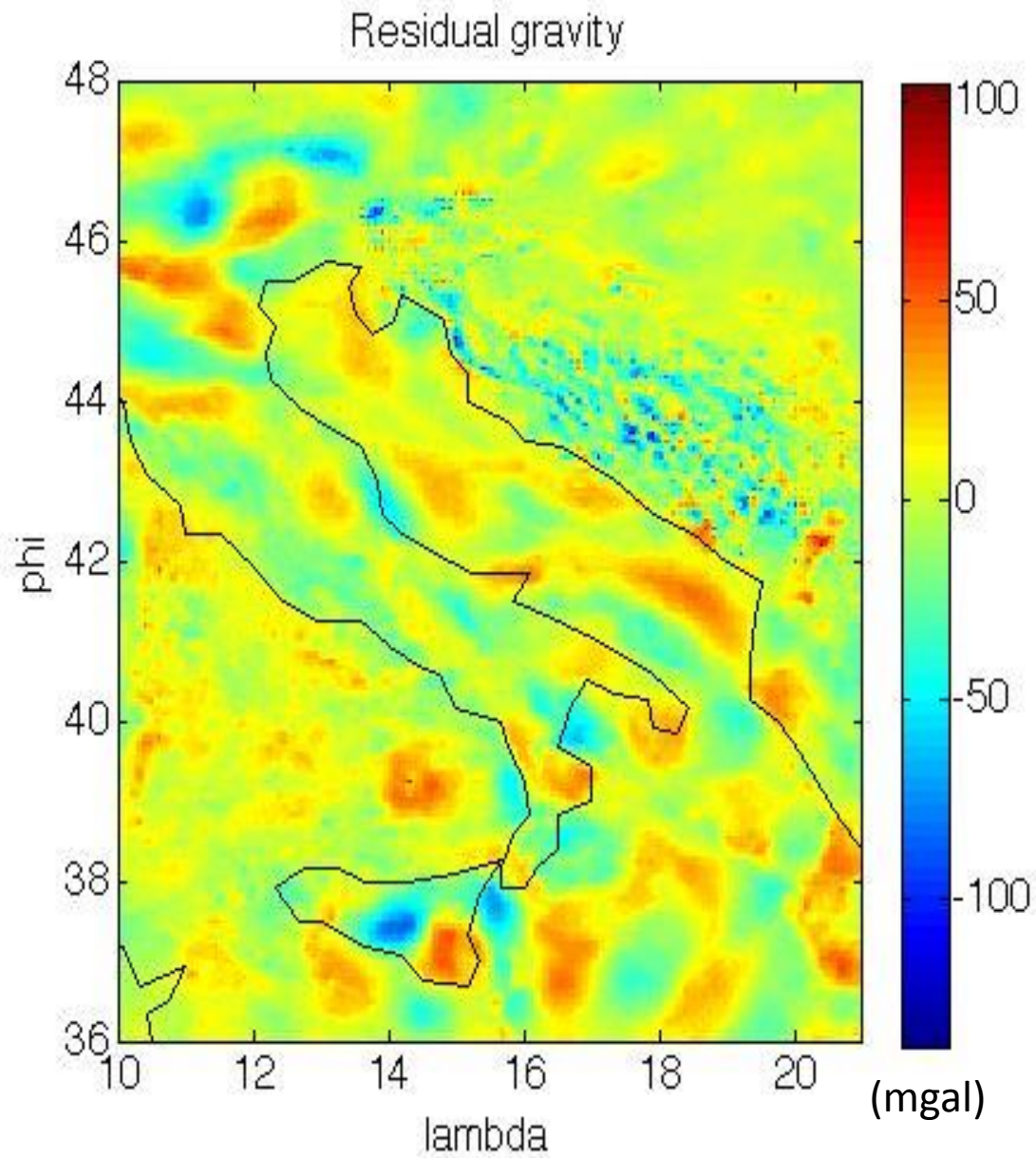
The statistics of the remove step

	Δg_{obs}	$\Delta g_{\text{R}} = \Delta g_{\text{obs}} - \Delta g_{\text{MOD}}$	$\Delta g_{\text{r}} = \Delta g_{\text{obs}} - \Delta g_{\text{MOD}} - \Delta g_{\text{RTC}}$
n	82657	82657	82657
E(mgal)	11.398	-4.835	-0.853
σ (mgal)	46.676	32.205	20.786
min(mgal)	-184.800	-245.144	-166.528
MAX(mgal)	267.710	216.964	119.615

The statistics of the gridded 3'×3' residual gravity

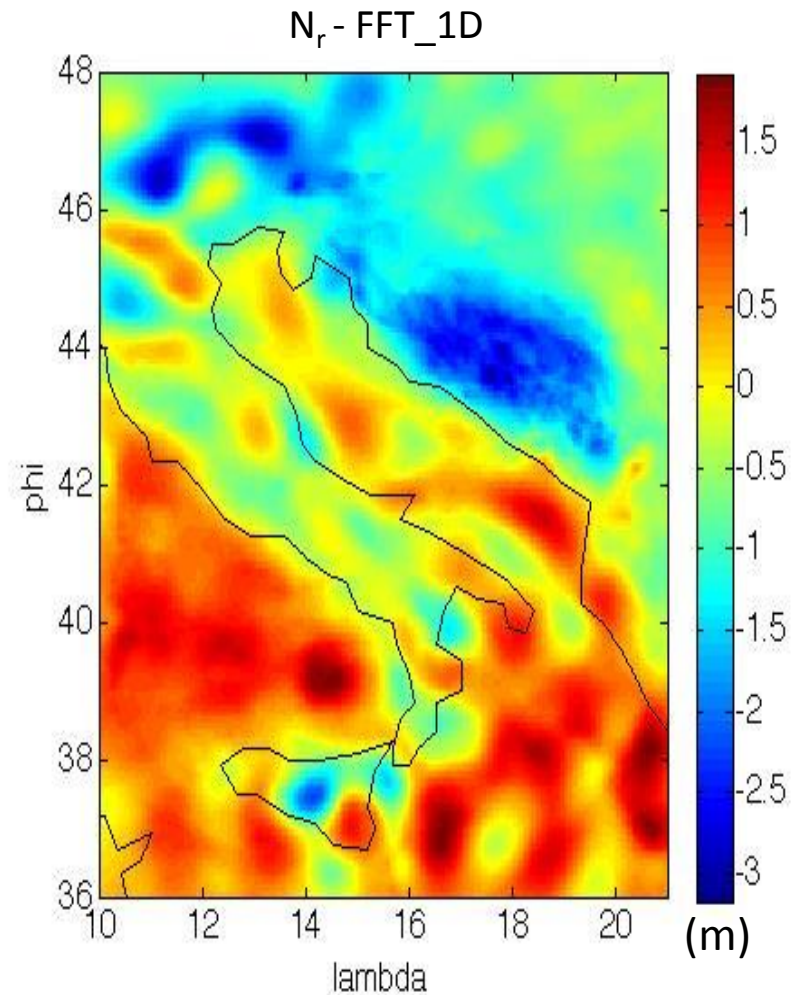
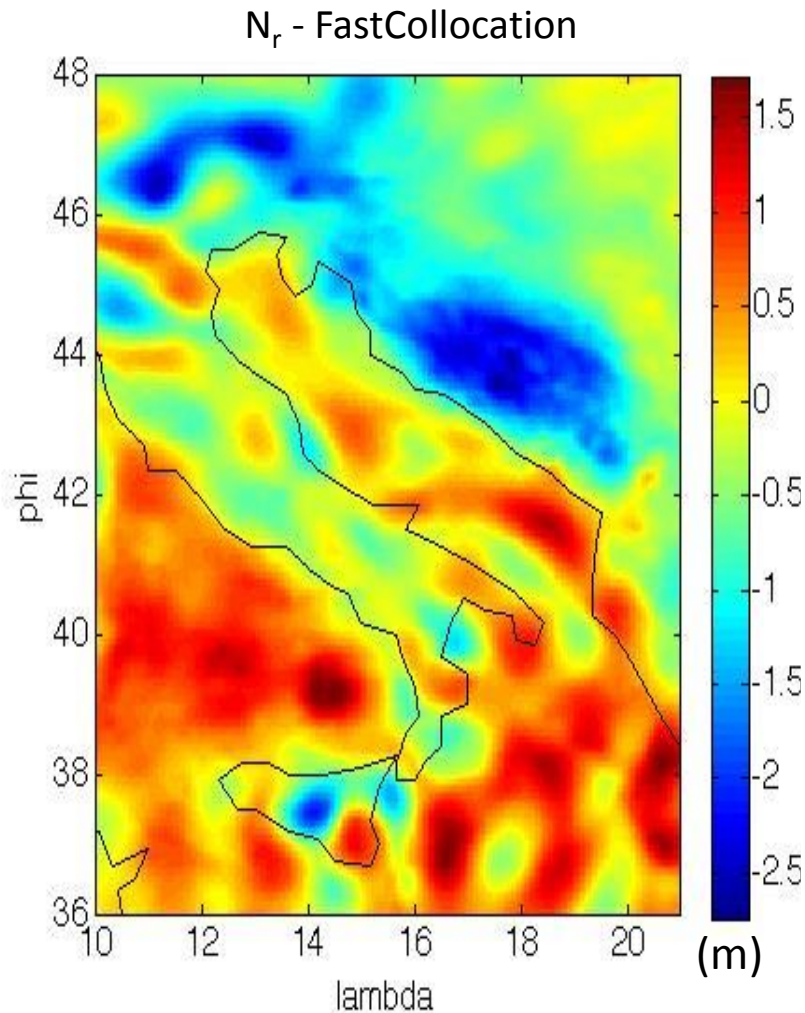
	$\Delta g_{\text{r}}(\text{GRID})$
n	53261
E(mgal)	-0.304
σ (mgal)	17.799
min(mgal)	-136.760
MAX(mgal)	104.801

The residual gravity field



The applied geoid estimation methods

- i) FastCollocation (Bottoni and Barzaghi, 1993)
- ii) Collocation (Lequentrec-Lalancette et al., 2002)
- iii) 1D_FFT (Haagmans et al., 1993)
- iv) 2D_FFT (Strang van Hess, 1990)



The residual geoid statistics

	N_r (FastCol)	N_r (Collocation)	N_r (1D_FFT)	N_r (2D_FFT)
n	53261	53261	53261	53261
E(m)	-0.148	-0.005	-0.200	-0.181
σ (m)	0.801	0.468	0.930	0.924
min(m)	-2.742	-2.267	-3.173	-3.136
MAX(m)	1.720	1.429	1.928	1.971

The statistics of the differences between N_r estimate: 1D_FFT vs FastCollocation

	$N_r(1D_FFT) - N_r(\text{FastCollocation})$
n	22701
$E(m)$	-0.061
$\sigma(m)$	0.117

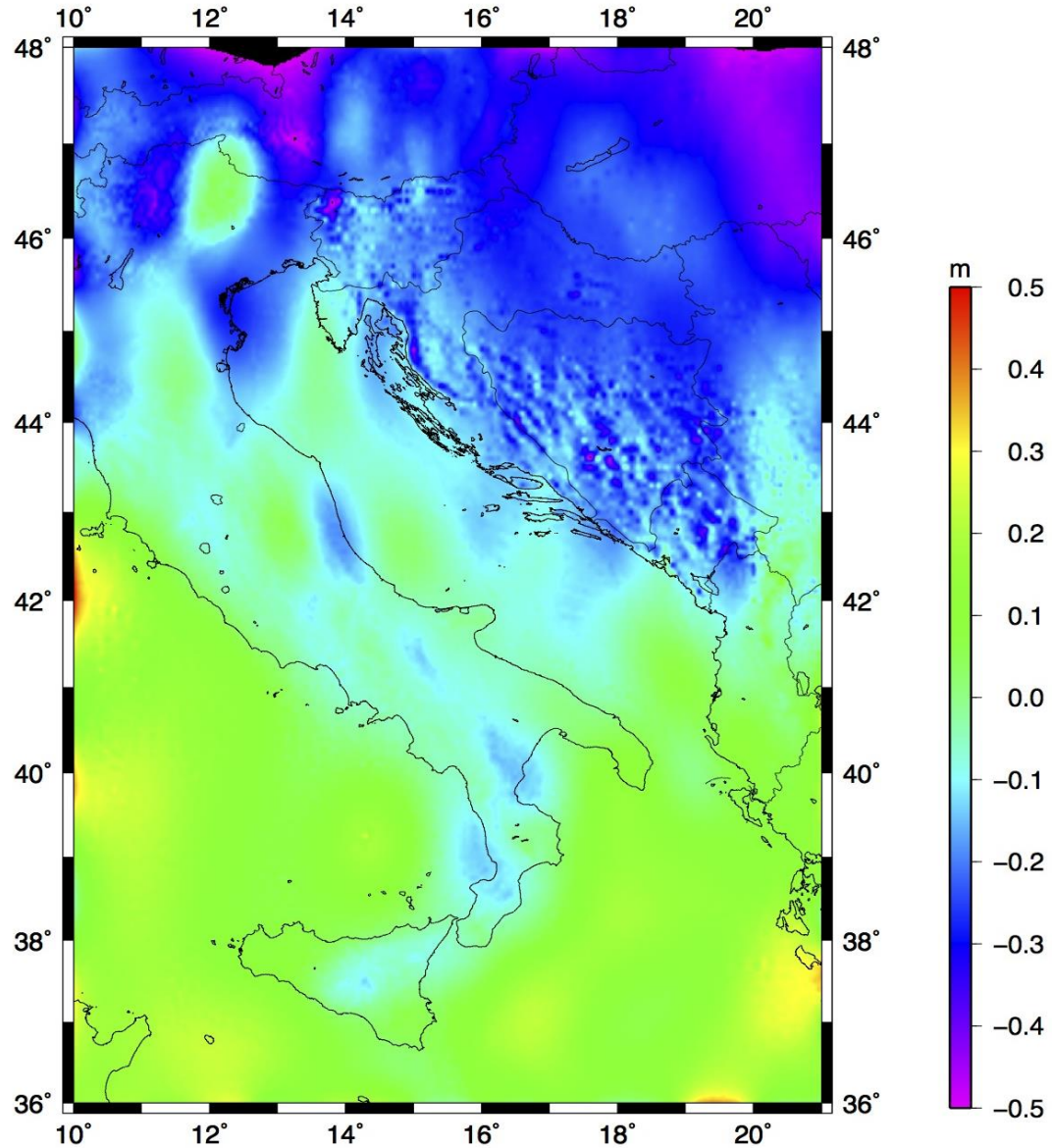
(In the area $38 < \varphi < 46$ $12 < \lambda < 19$)

The statistics of the differences between N_r estimates: 1D_FFT vs 2D_FFT

	$N_r(1D_FFT) - N_r(2D_FFT)$
n	22701
$E(m)$	-0.019
$\sigma(m)$	0.016

(In the area $38 < \varphi < 46$ $12 < \lambda < 19$)

The differences between N_r estimates: 1D_FFT vs FastCollocation



The statistics of the differences w.r.t. GPS/lev points

$$v = (N_{grav} - N_{GPS/lev}) - DN(q, l) = (N_{grav} - N_{GPS/lev}) - dx \sin q \cos l + dy \sin q \sin l + dz \cos q$$

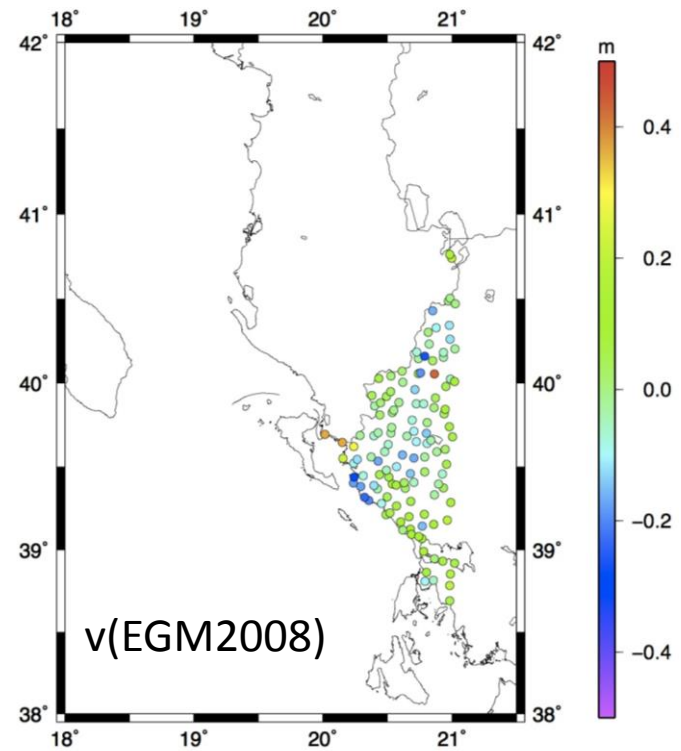
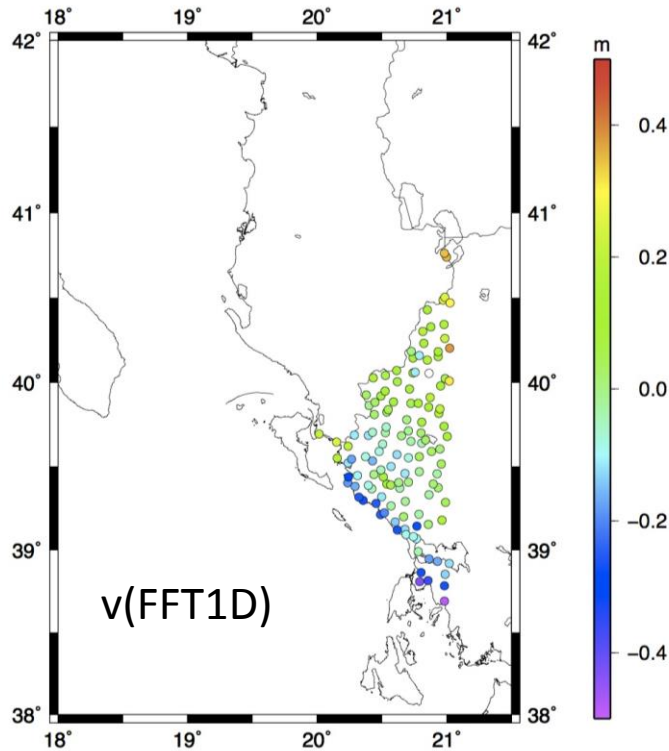
$q = 90^\circ - j$; $N_{GPS/lev} = h - H$ *(dx, dy, dz) datum shift translation*

Italy (mainland)

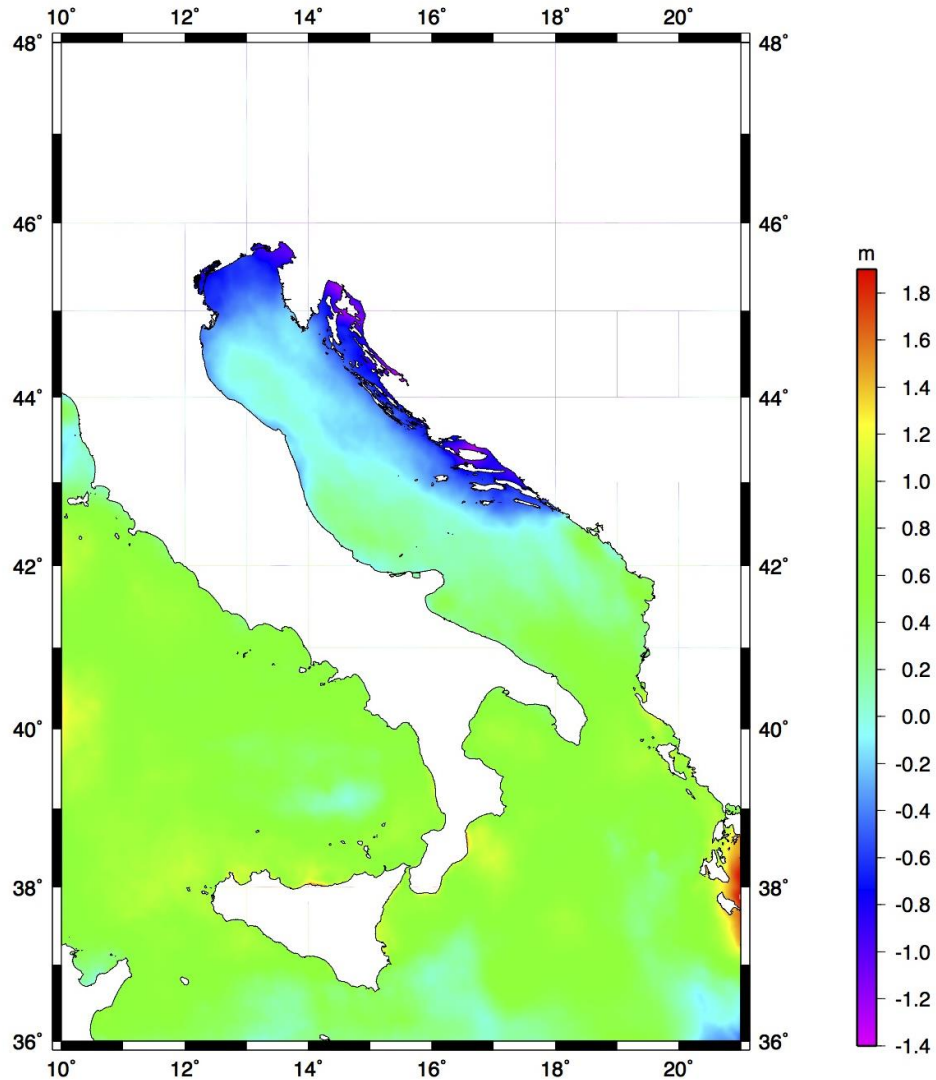
	v(FASTCOL)	v(1DFFT)	v(EGM2008)
n	594	590	595
E(m)	0.000	0.000	0.000
σ (m)	0.095	0.084	0.084
min(m)	-0.243	-0.294	-0.227
MAX(m)	0.260	0.239	0.276

Greece

	v(FASTCOL)	v(1DFFT)	v(EGM2008)
n	126	126	126
E(m)	0.000	0.000	0.000
σ (m)	0.181	0.164	0.118
min(m)	-0.489	-0.485	-0.304
MAX(m)	0.547	0.545	0.434



The DOT in the Adriatic Sea
based on
the DTU2013 MSS and the 1D_FFT geoid estimate



Comments and conclusions

- The Adriatic Sea Test proved that further checks on the gravity data are needed (consistency among different gravity databases)
- The processing chain seems to be satisfactory but some refinements must be implemented (possibly a denser gravity database should be selected based on a 1'x1' selection grid)
- The GOCE-DIR5 GGM allows an effective data reduction; other solutions will be also tested in the future (e.g. the time-wise and the space-wise solutions)
- Differences in the geoid computation methods are quite large and, to some extent, unexpected (ad hoc analysis will be devised to come to more coherent solutions)